

FFA'20, TRIUMF

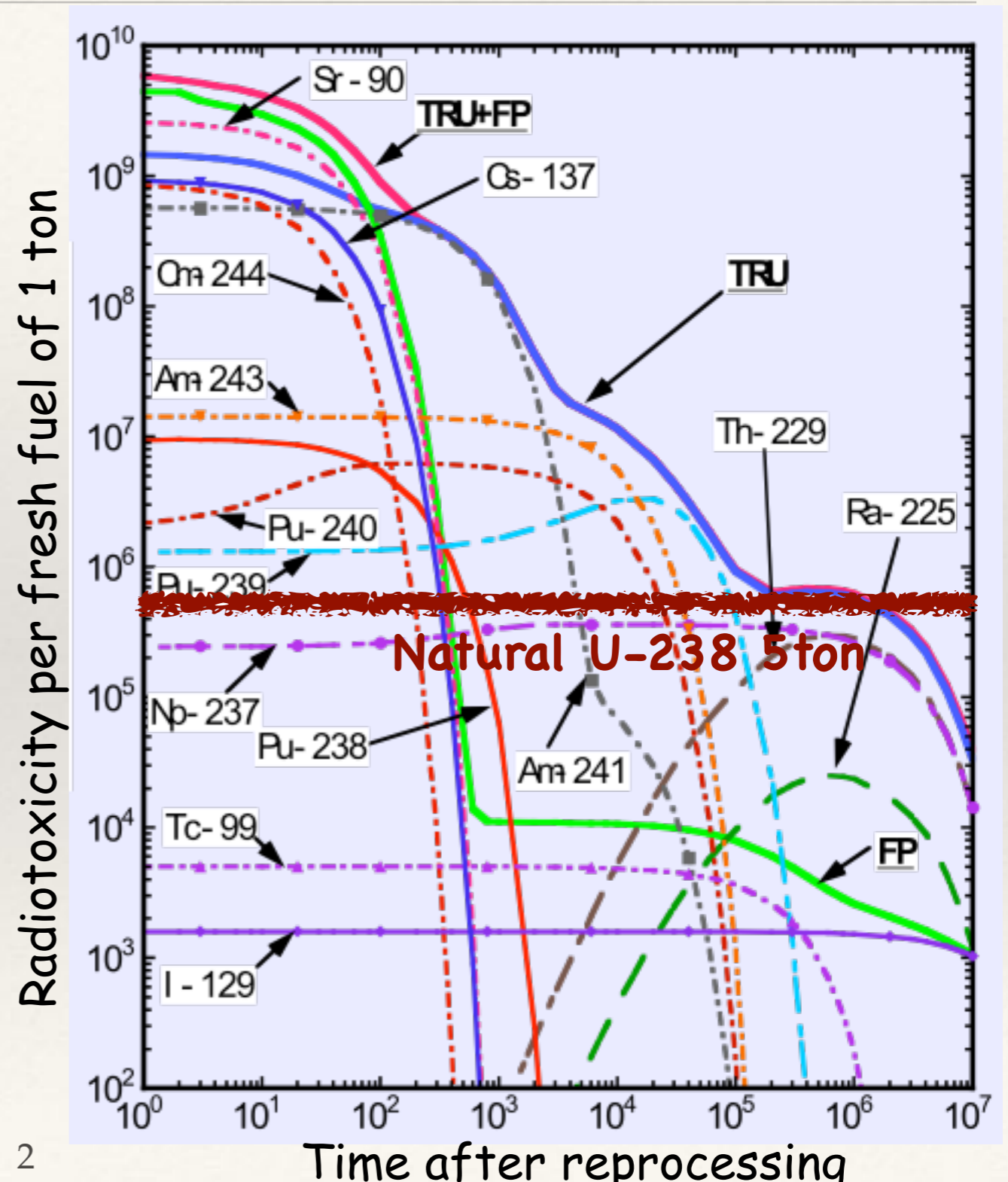
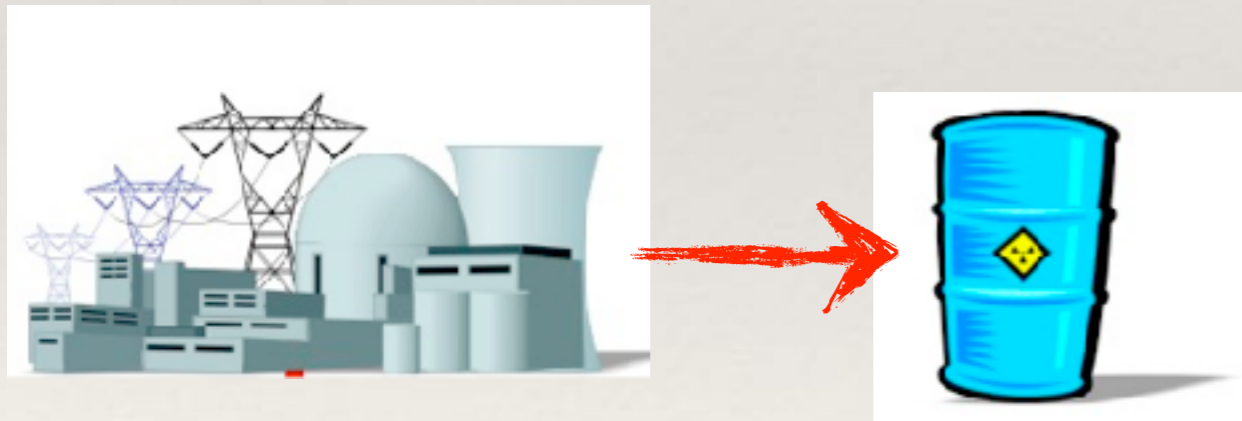
Applications of ERIT_FFA

-Mitigation of long-lived nuclear wastes—

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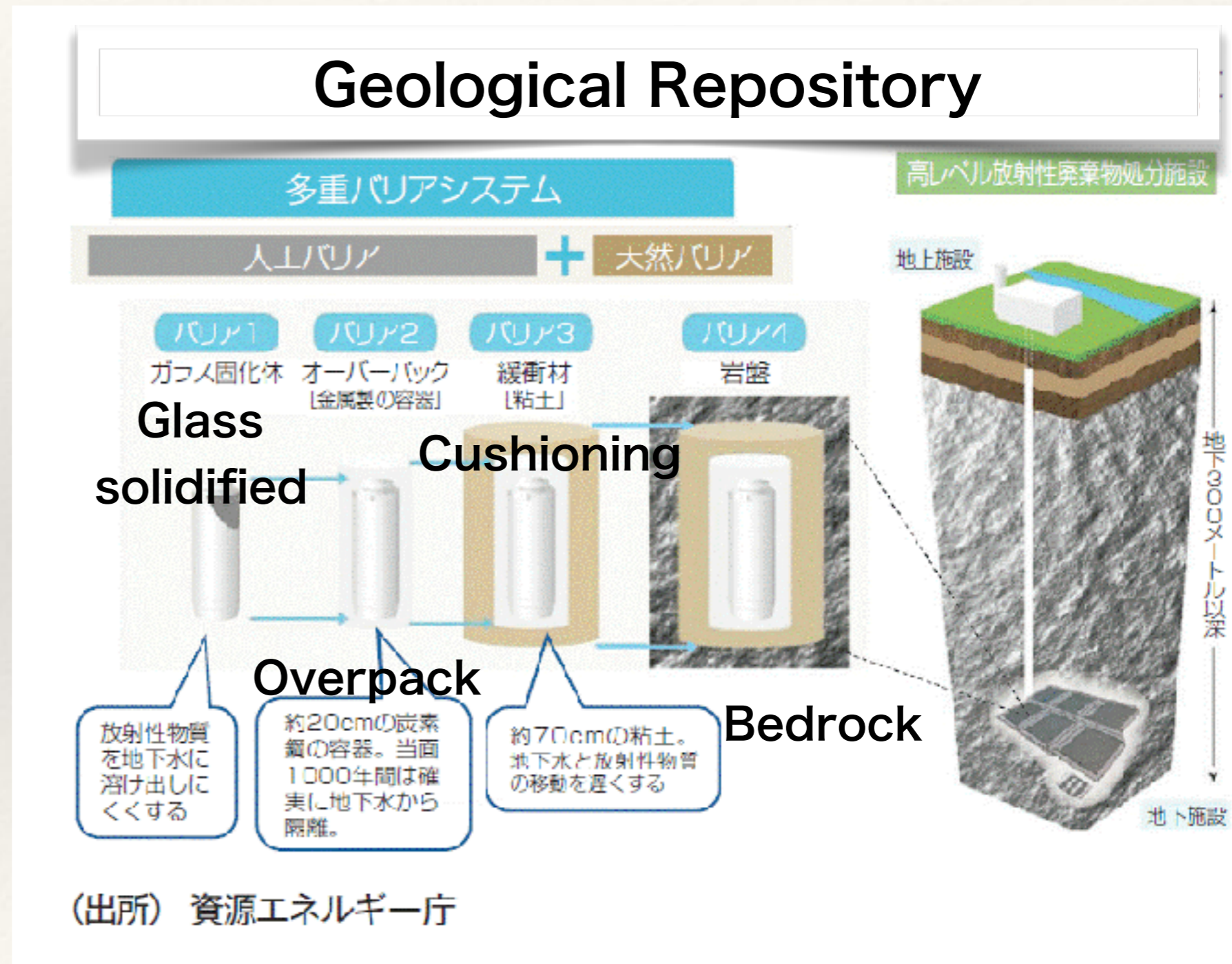
Radio toxicity from long-lived nuclear wastes

- ❖ 1GWh nuclear plant
- ❖ Fresh fuel : U(3%-enriched)
~300ton



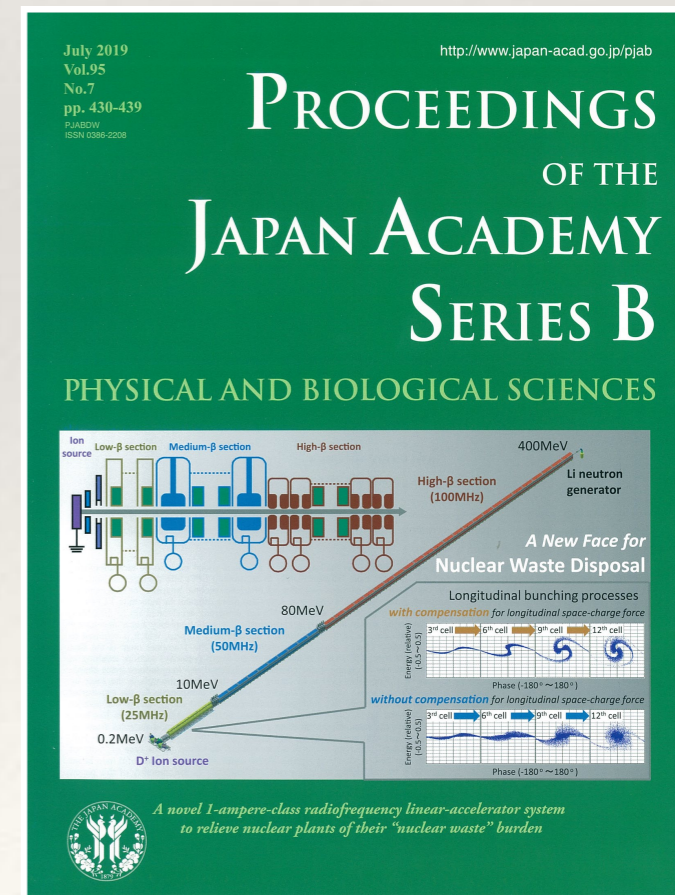
Geological repository

- ❖ Amount of long-lived nuclear wastes generated in one year of operation at 1-GWh nuclear plant
 - ❖ LLFPs(Long lived fission products):
 - ❖ Tc-99, I-129 , etc
 - ❖ 12kg/year
 - ❖ MA(minor actinides)
 - ❖ Np-237,Am-241
 - ❖ 6kg/year



NX:Nuclear Transmutation

- ❖ Neutron induced nuclear transmutation:NNX
 - ❖ Transform the radioactive nuclei(LLFP and MA) in stable or short lived nuclei.→ ADS can treat MA but not LLFP efficiently.
 - ❖ Require, however, a large neutron flux for LLFP and MA.
 - ❖ High power deuteron accelerator: **1A-200MeV/u(400MW)!**
 - ❖ cf. 'Proposal of a 1-ampere-class deuteron single-cell linac for nuclear transmutation', **Proc.Jpn.Acad.Ser.,B95(2019)430.**
- ❖ **Muons Catalyzed Fusion(MuCF) mitigate the beam power → 1/5-1/10**
 - ❖ 14-MeV neutrons produced by **MuCF** chain reactions.
 - ❖ Transmute the long-lived FPs(fission product) and MAs(Minor Actinide) with $<1/5$ of the electric power generated by a nuclear plant.



MuCF: Muon Catalyzed Fusion

❖ MuCF process

1. μ^- absorption into D-T mixture

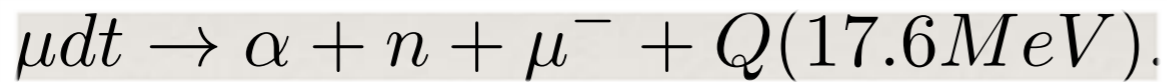
2. μdt molecule formation

❖ Formation rate $\sim 0.5 \times 10^9 / s$

$\rightarrow \sim 1,000 \mu dt$ molecules per muon life ($2.1 \mu s$).

❖ Fusion reaction

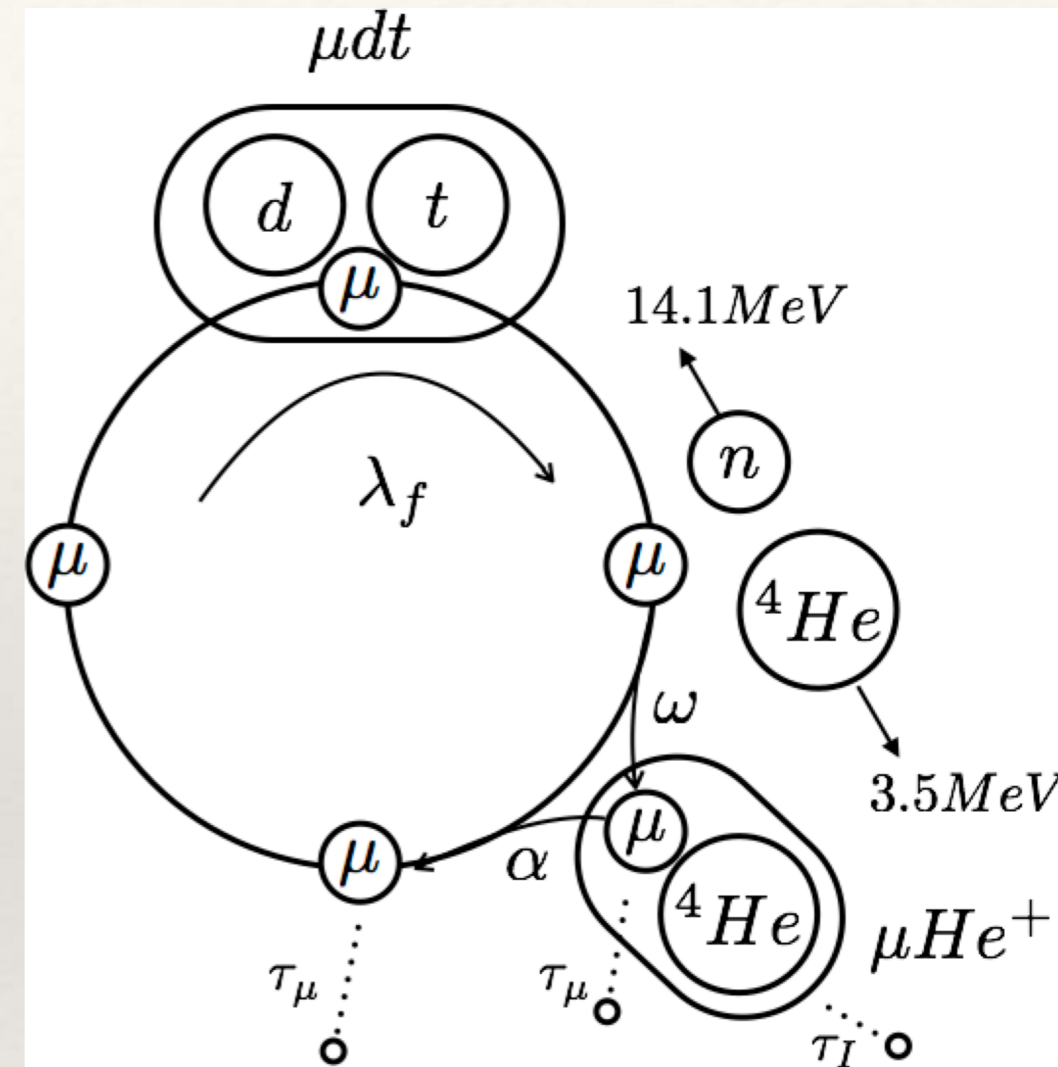
❖ Distance of d-t: $\sim 1/200$



3. Chain cycle

❖ $\omega \sim 0.6-0.7\% \rightarrow N_c \sim 100-150$ fusion/ μ

❖ **100-150 neutrons/single negative muon**



$$N_c = \left[\frac{1}{\lambda_f \tau_\mu} + \frac{\omega}{\lambda_f} \right]^{-1}$$

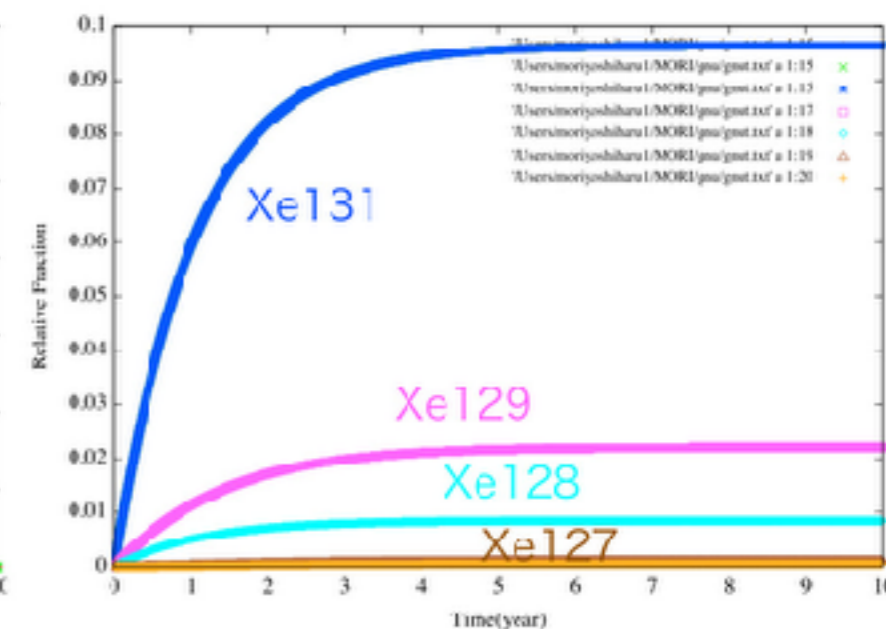
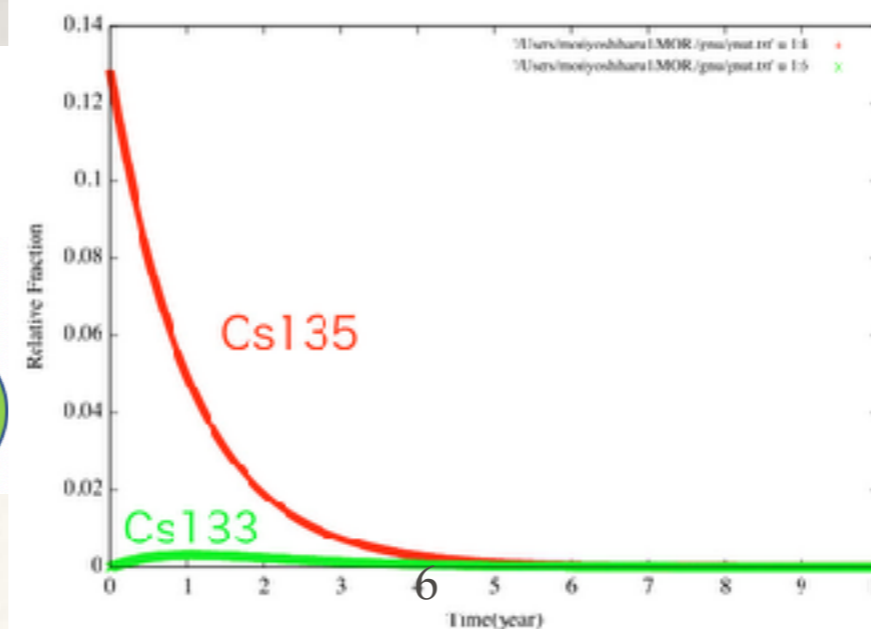
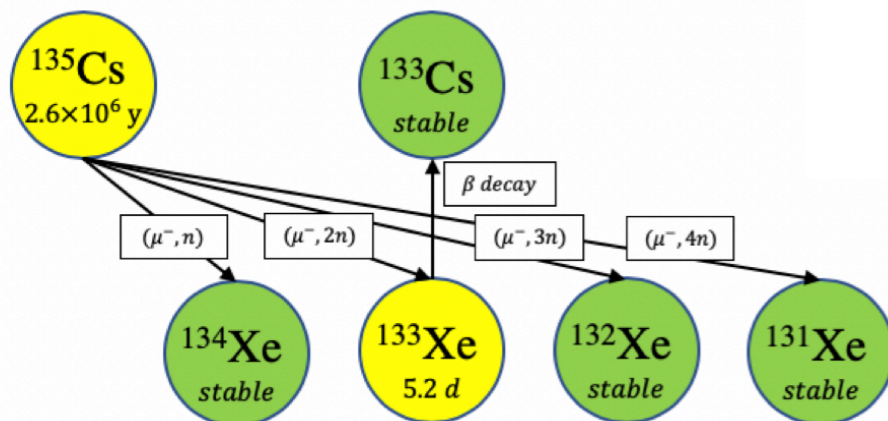
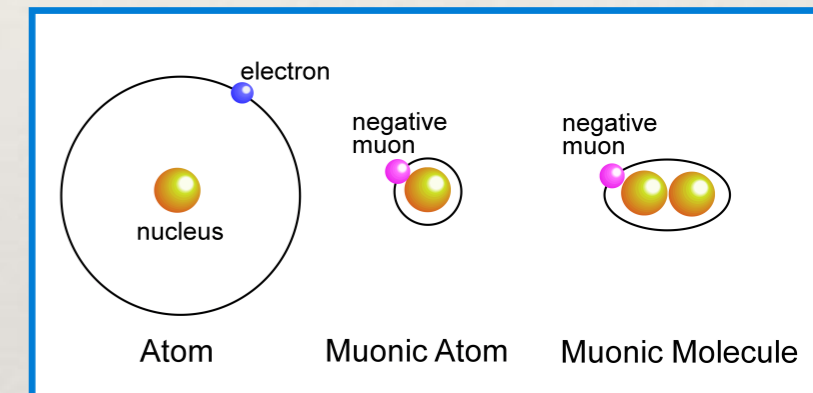
Muon Nuclear Transformation

- ❖ Nuclear transformation in muonic atom
 - ❖ 1st: Formation μ _atom \rightarrow 2nd: Nuclear transmutation

$$a_{\mu} = \left(\frac{1}{207} \right) \times Z^{-1} \times 10^4 \text{ fm.}$$

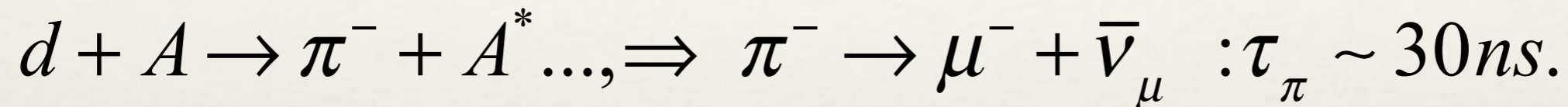
$$R = 1.2 \times A^{1/3} \text{ fm.}$$

- ❖ Transmutation probability $\rightarrow >95\%$ for $Z > 30$ nuclei.
- ❖ Radioactive nuclei such as Cs-135 which are inadequate for neutron.



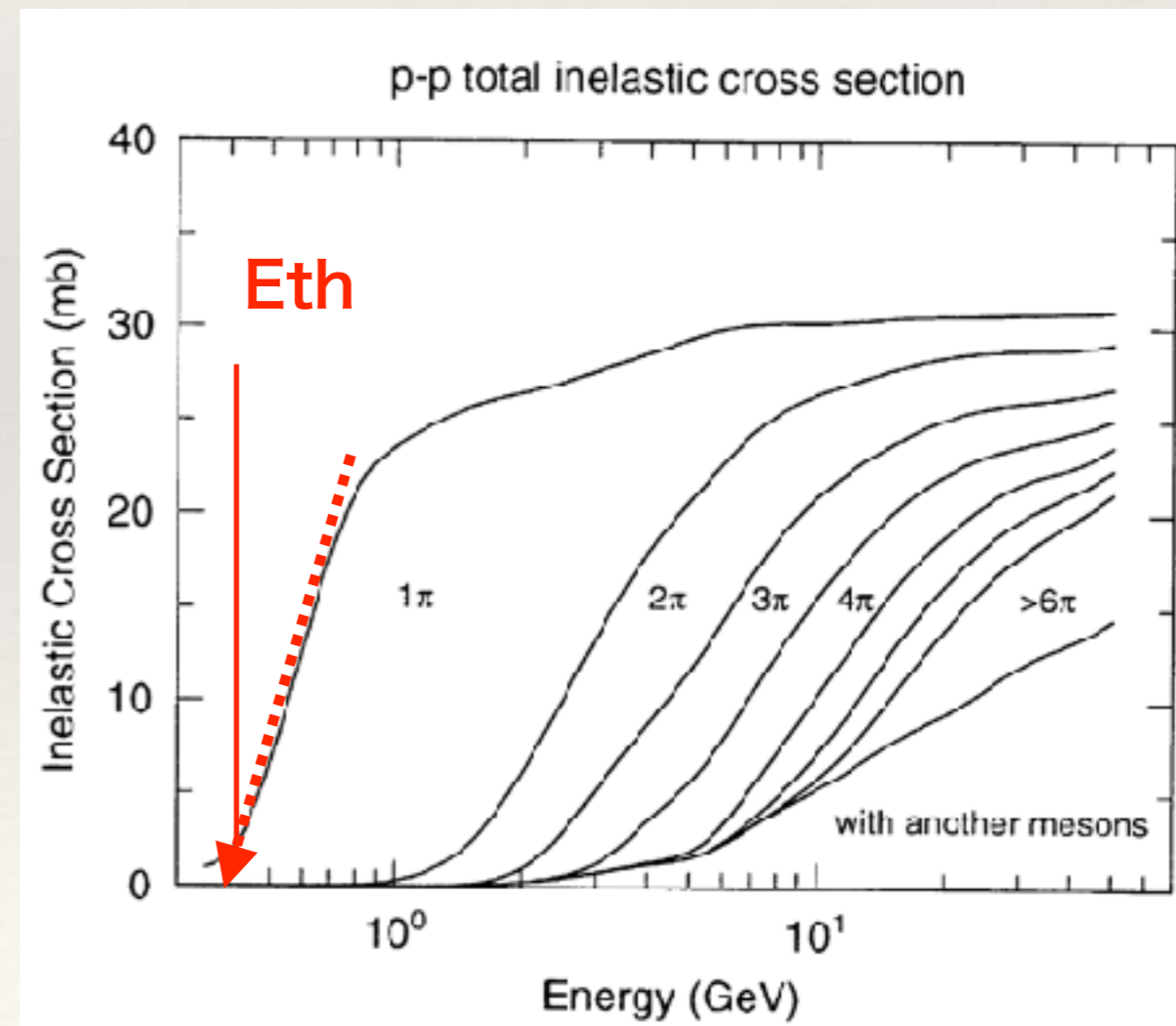
Negative Muon Production

- ❖ Pion production and decaying to μ^-



- ❖ Threshold energy **>250MeV/u**
- ❖ Cross section: very energy dependent

$$\sigma_{\pi^-} \approx 10\text{mb at } 400\text{MeV/u.}$$



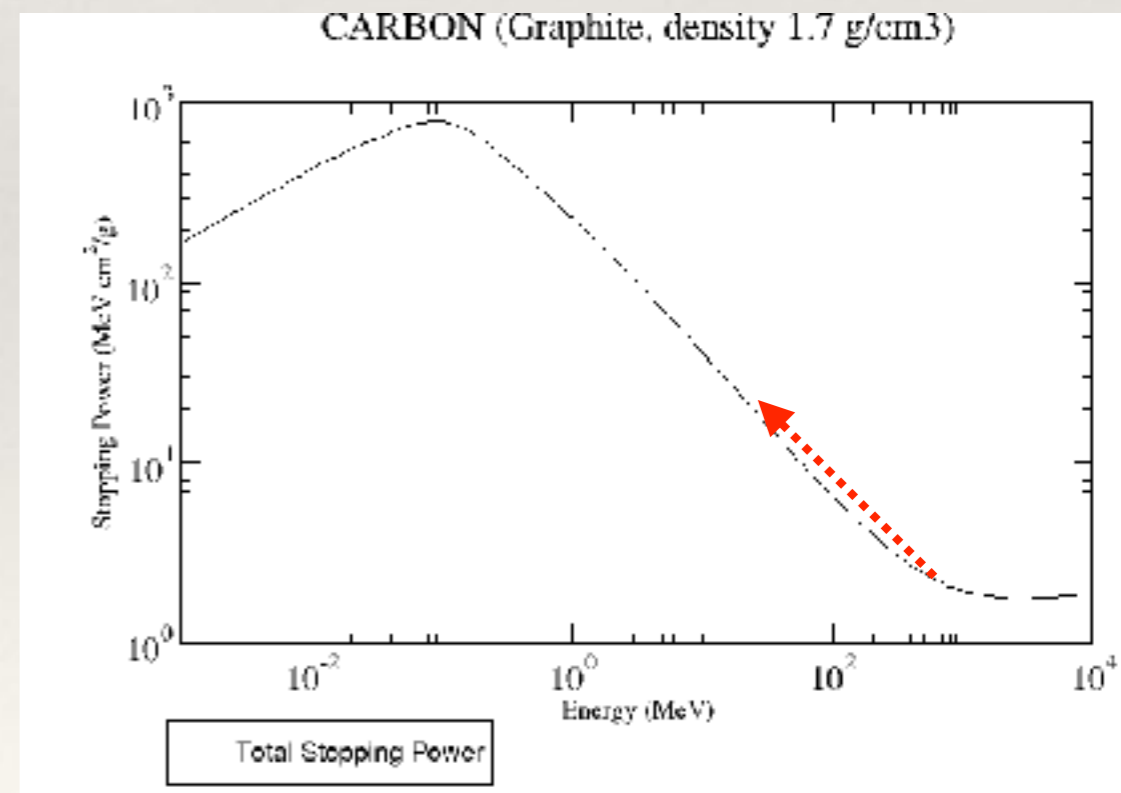
Efficiency of Particle Production

- ❖ Difficulties for π^- production
 - ❖ σ_π depends on the energy. \rightarrow energy loss of the projectile particle by ionization of target
 - ❖ Absorption of π^- in the target
- ❖ Efficiency of particle production

$$\eta \approx 1 - \exp \left[- \int_{E_f}^{E_i} \frac{\sigma(E) n}{S(E)} dE \right]$$

- ❖ cf, 500MeV / u, d-beam, Li target

$$\eta < 0.1 \Leftrightarrow \int_{E_f}^{E_i} \frac{\sigma(E) n}{S(E)} dE < 0.1$$



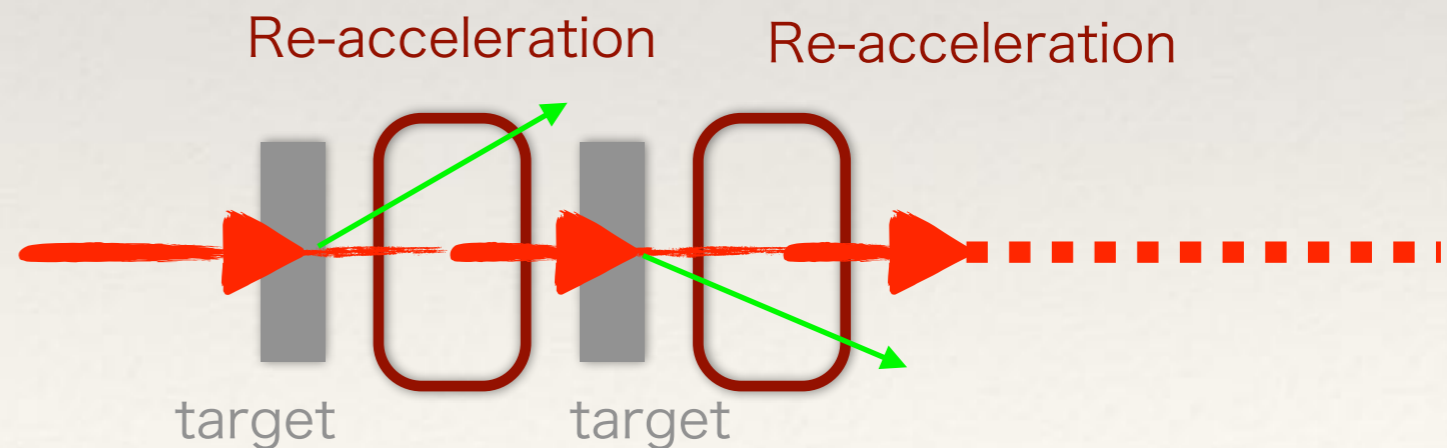
Energy Recovery Scheme

- ❖ Efficiency of particle production

$$\eta \approx 1 - \exp \left[- \int_{E_f}^{E_i} \frac{\sigma(E)n}{S(E)} dE \right], \quad S(E) : \text{stopping power.}$$

- ❖ If $S(E)$ can be effectively zeroed, η becomes 1.
- ❖ The energy loss at the target recovers by re-accelerating.

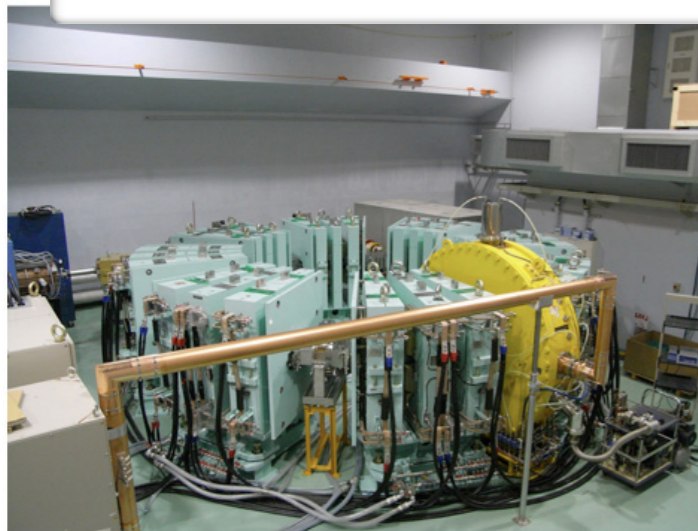
$$\eta \approx 1 \Leftarrow S(E) \doteq 0$$



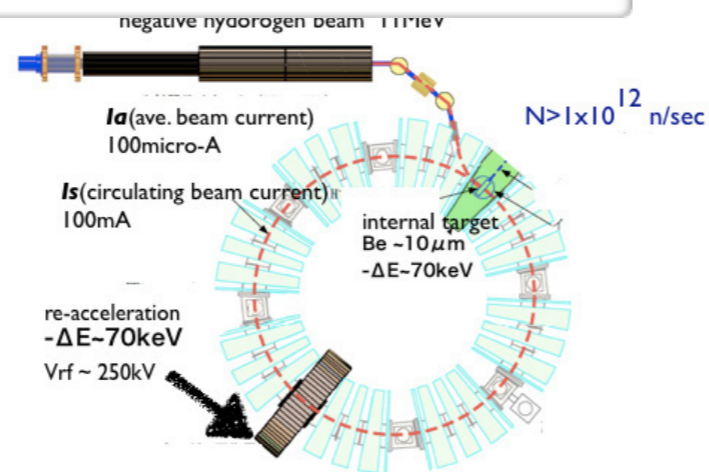
ERIT (Energy Recovery Internal Target) ring

- ❖ Principle of ERIT
 - ❖ Storage ring and thin target
 - ❖ Energy recovery by rf re-acceleration
 - ❖ Ionization cooling
- ❖ Requirements for ring performance
 - ❖ Large energy and transverse acceptances → FFA

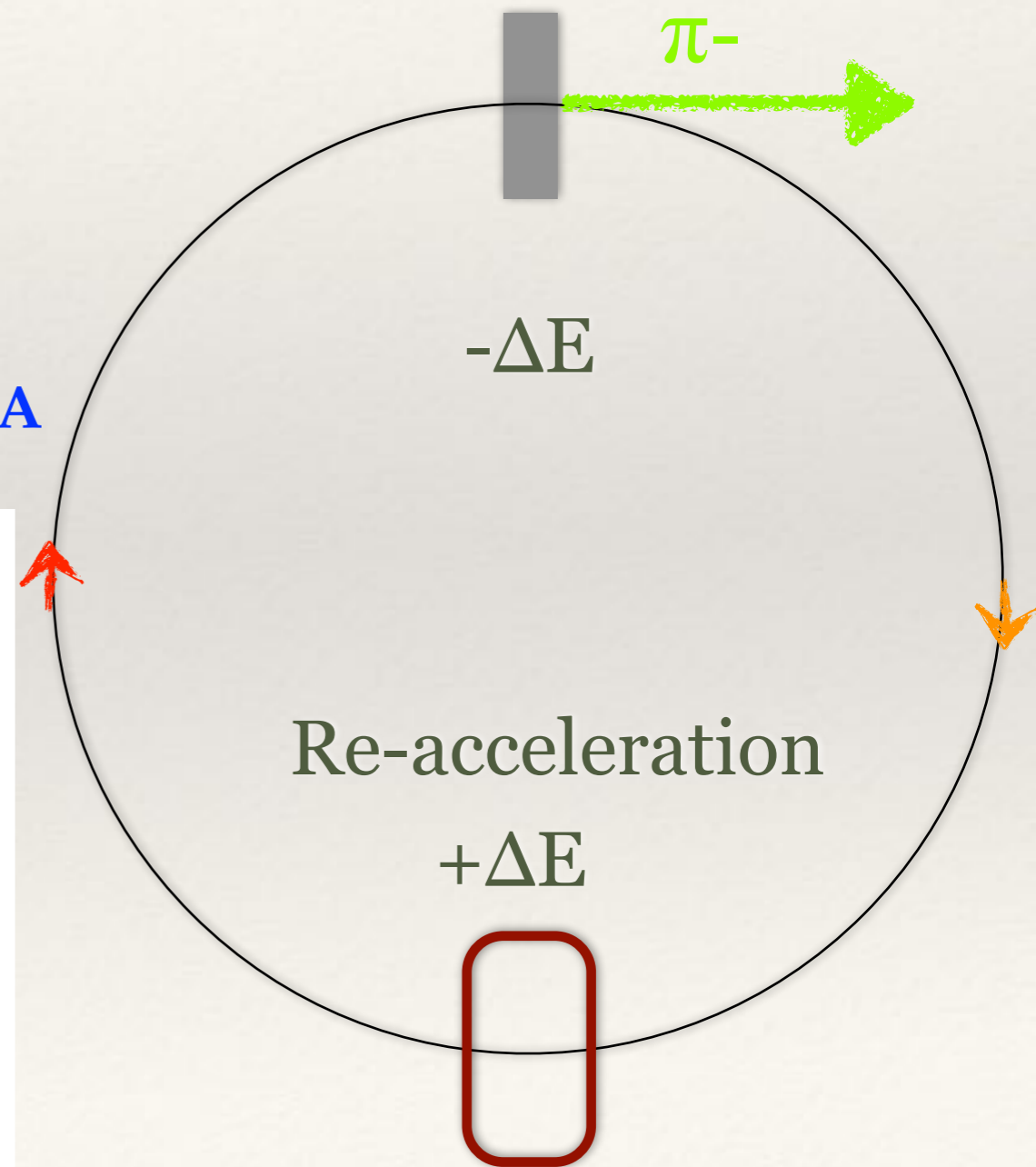
Demonstration: neutron source



(a)



(b)



Multiplex ERIT:MERIT

❖ MERIT : Hybrid ring for beam acceleration and circulation on target

❖ Acceleration: fixed rf frequency

❖ Serpentine path rf bucket

$$\alpha \sim \frac{1}{\gamma_s^2} = \frac{1}{k+1}$$

❖ Circulation: wedged target

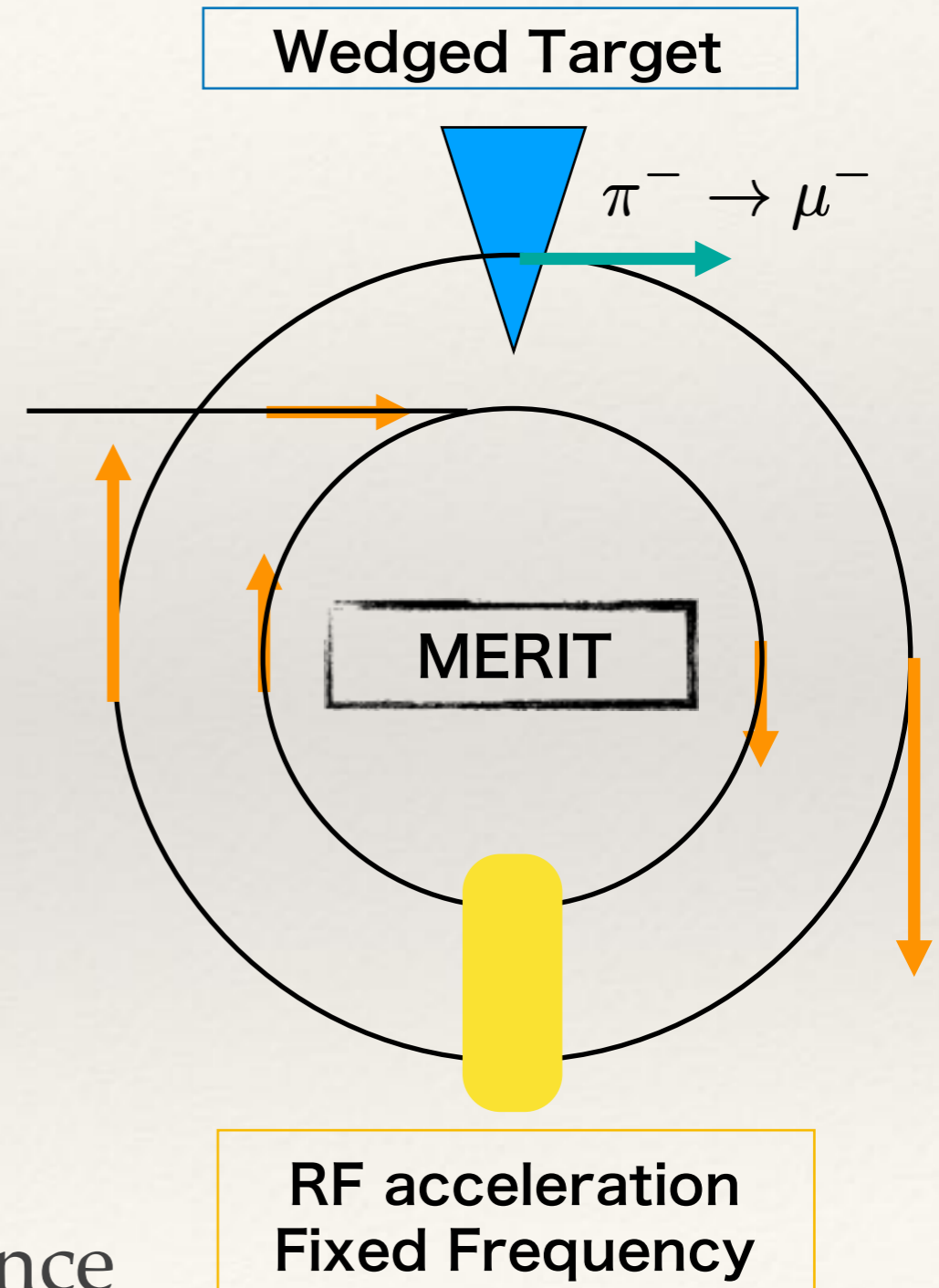
$$\frac{\Delta E}{l(E)} + S(E) \approx 0.$$

ΔE : energy gain per turn

$S(E)$: stopping power

$l(E)$: target thickness

❖ Ionization cooling: modest acceptance



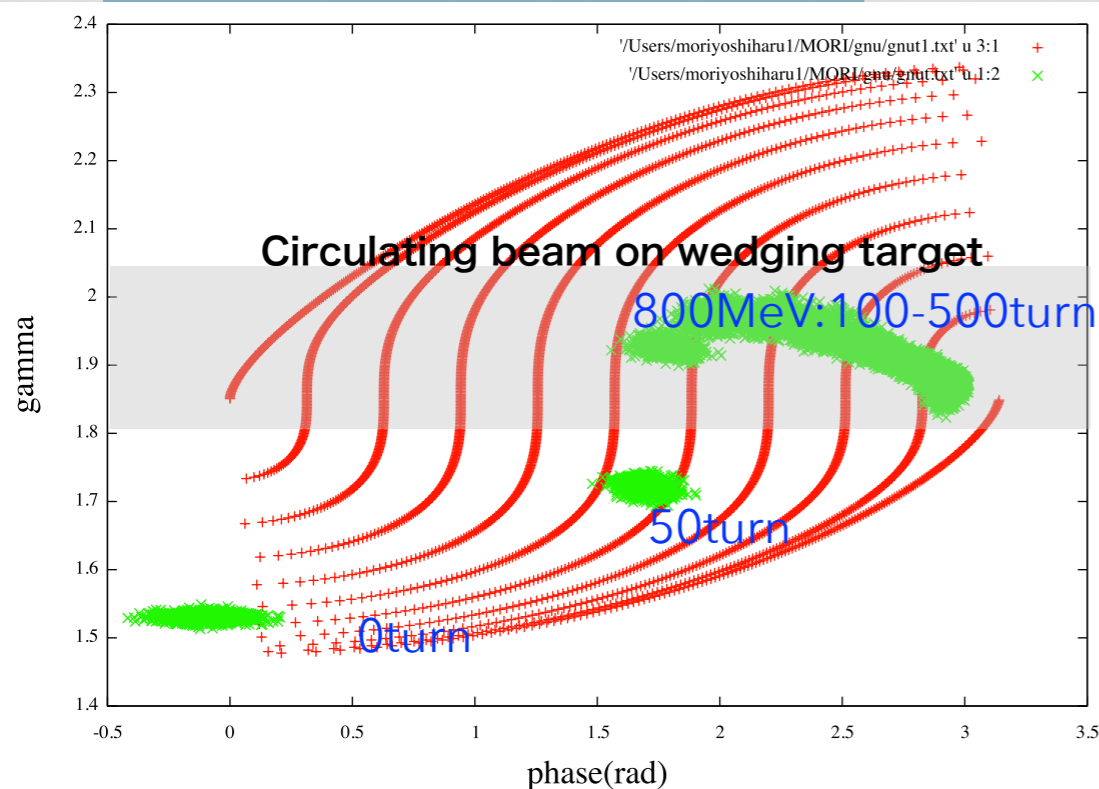
MERIT : π/μ production ring(1)

❖ Proton

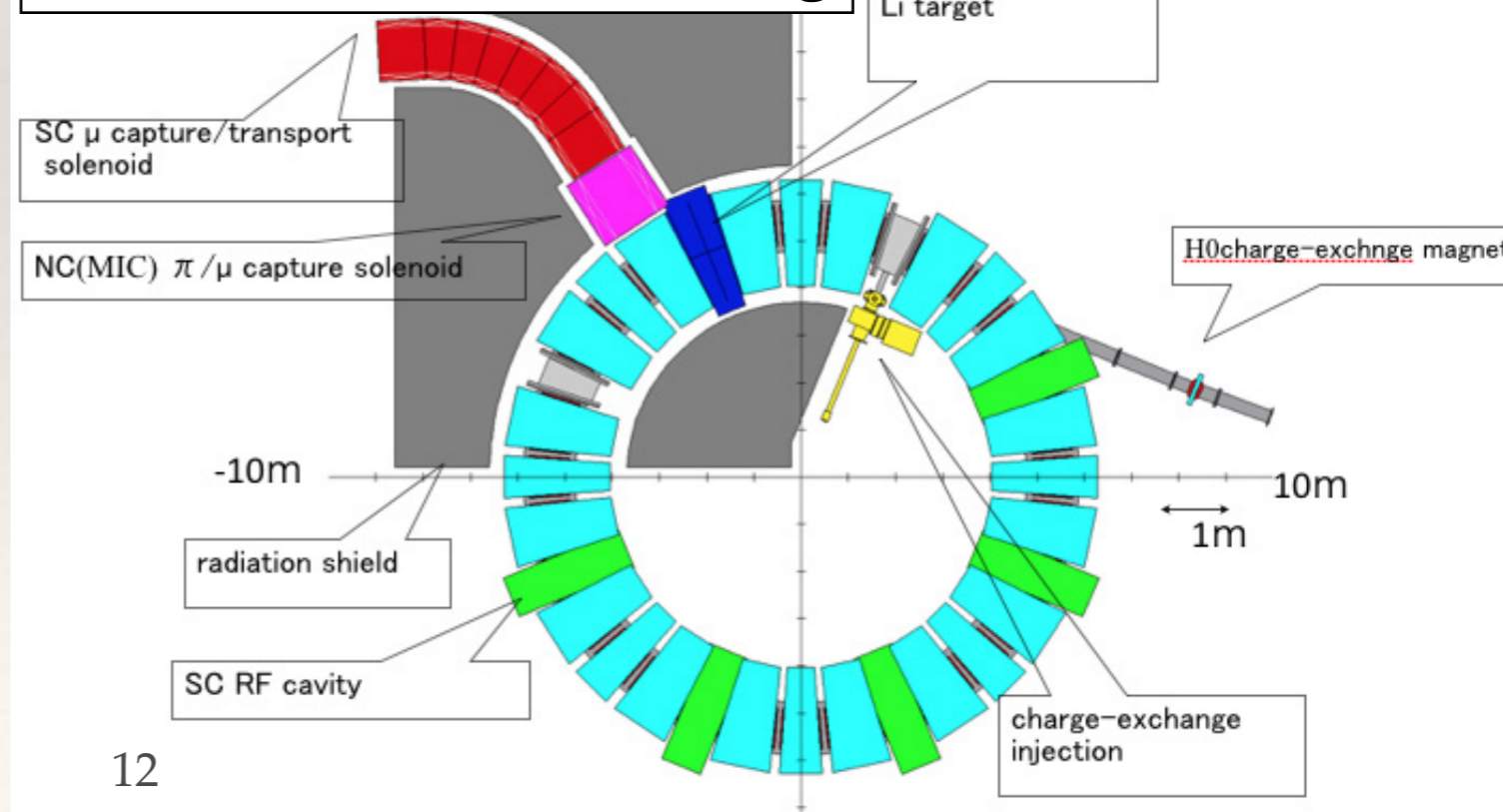
- ❖ Acceleration : 500MeV - 800MeV
- ❖ Circulation on target : 800MeV for π production

Ring configuration H-FFAG
 Energy range(MeV) 500-800
 Magnetic rigidity(T.m) 3.633 -4.877
 Lattice FDF
 Average radius(m) 5.044-5.5
 Magnetic field(T):F 1.96-2.41
 Magnetic field(T):D 1.71-2.11
 Number of cell 8
 Geometrical field index 2.43
 Cell tune:H 0.212
 Cell tune:V 0.180
 Beta function(m) @SS:H 2.5
 Beta function(m) @SS:V 2.8
 Dispersion function(m) 1.5

Serpentine Acceleration



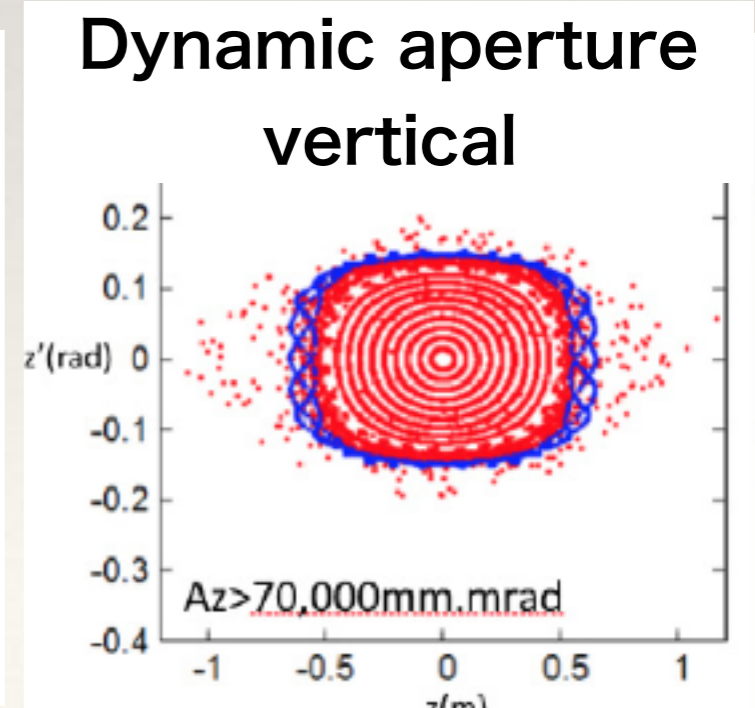
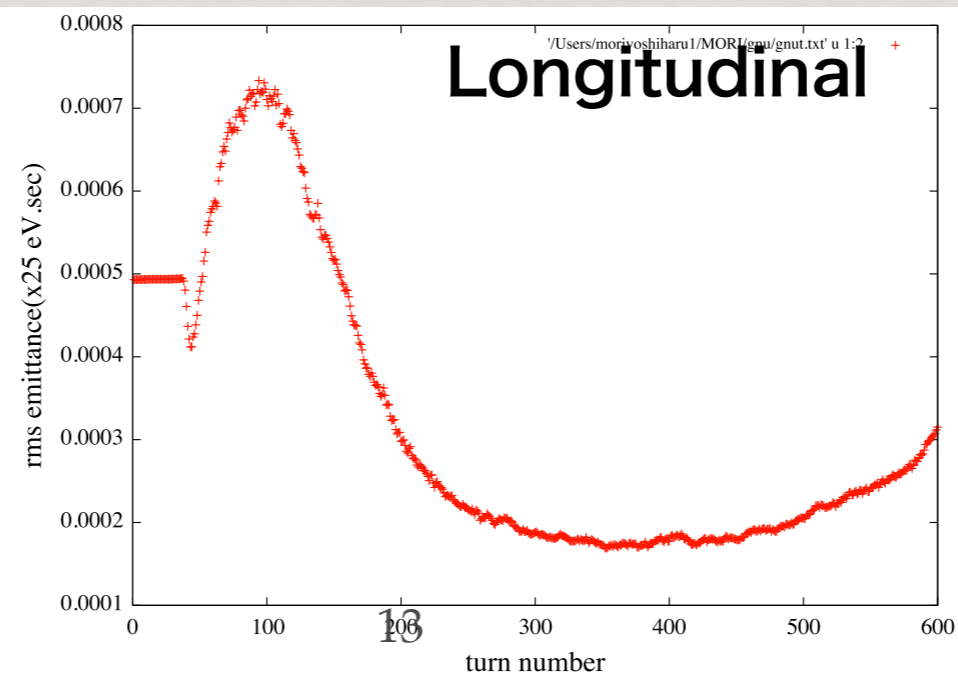
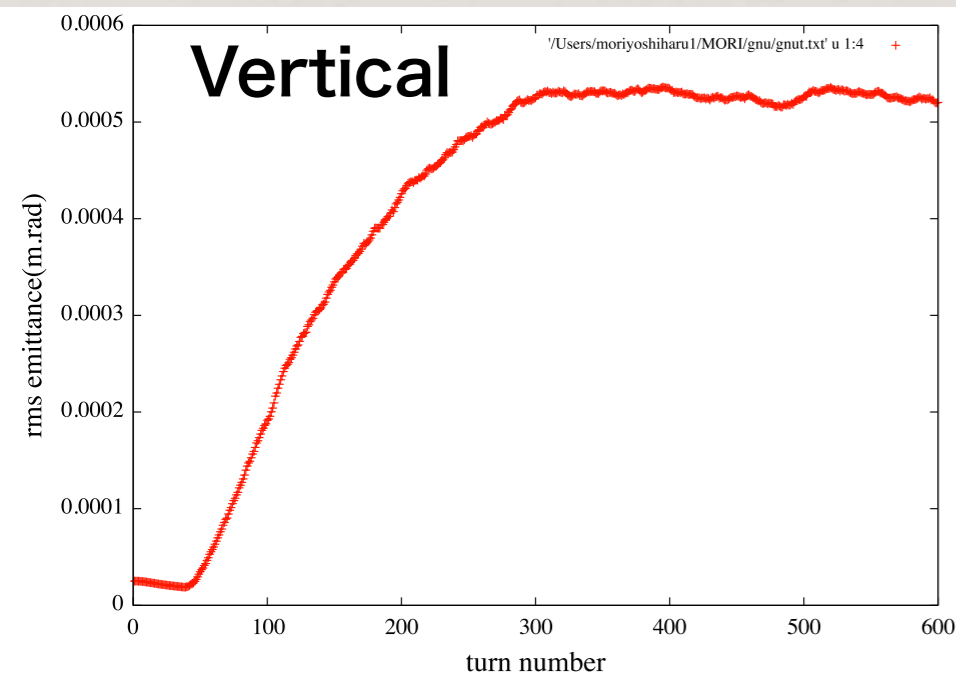
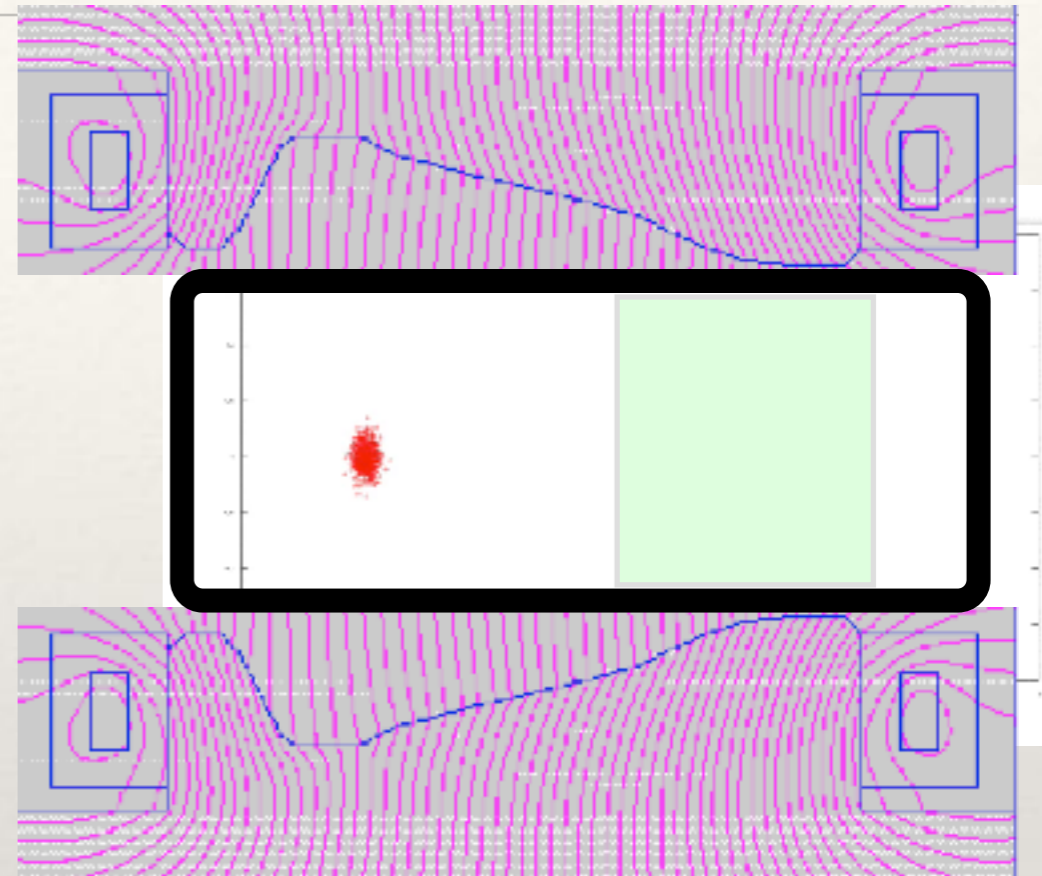
400-800 MeV MERIT ring



MERIT : π/μ production ring(2)

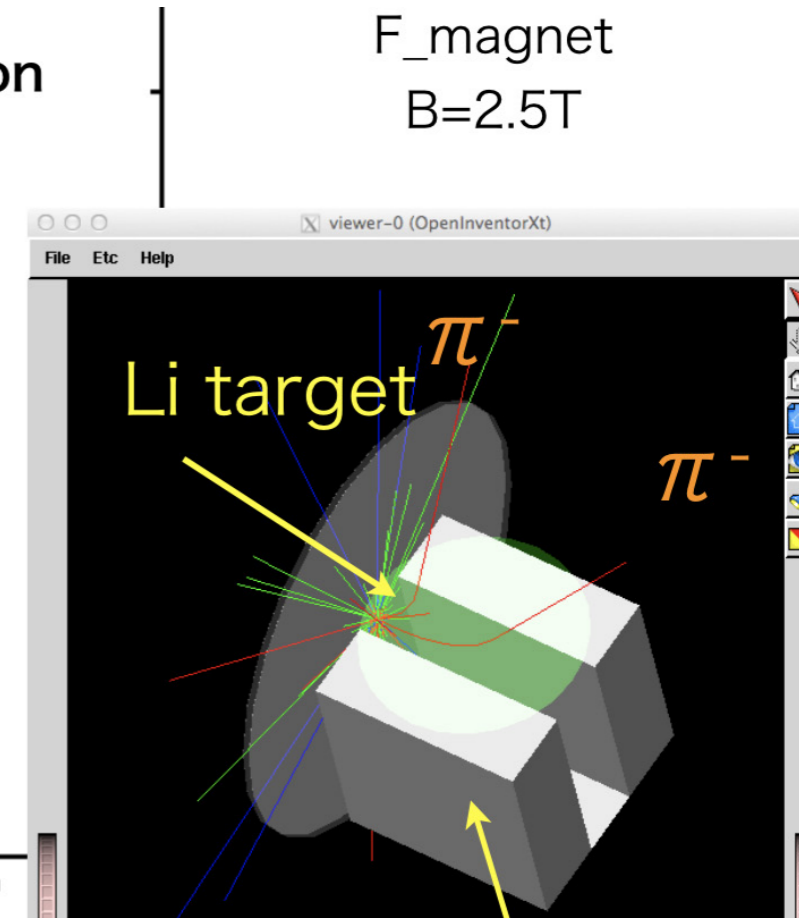
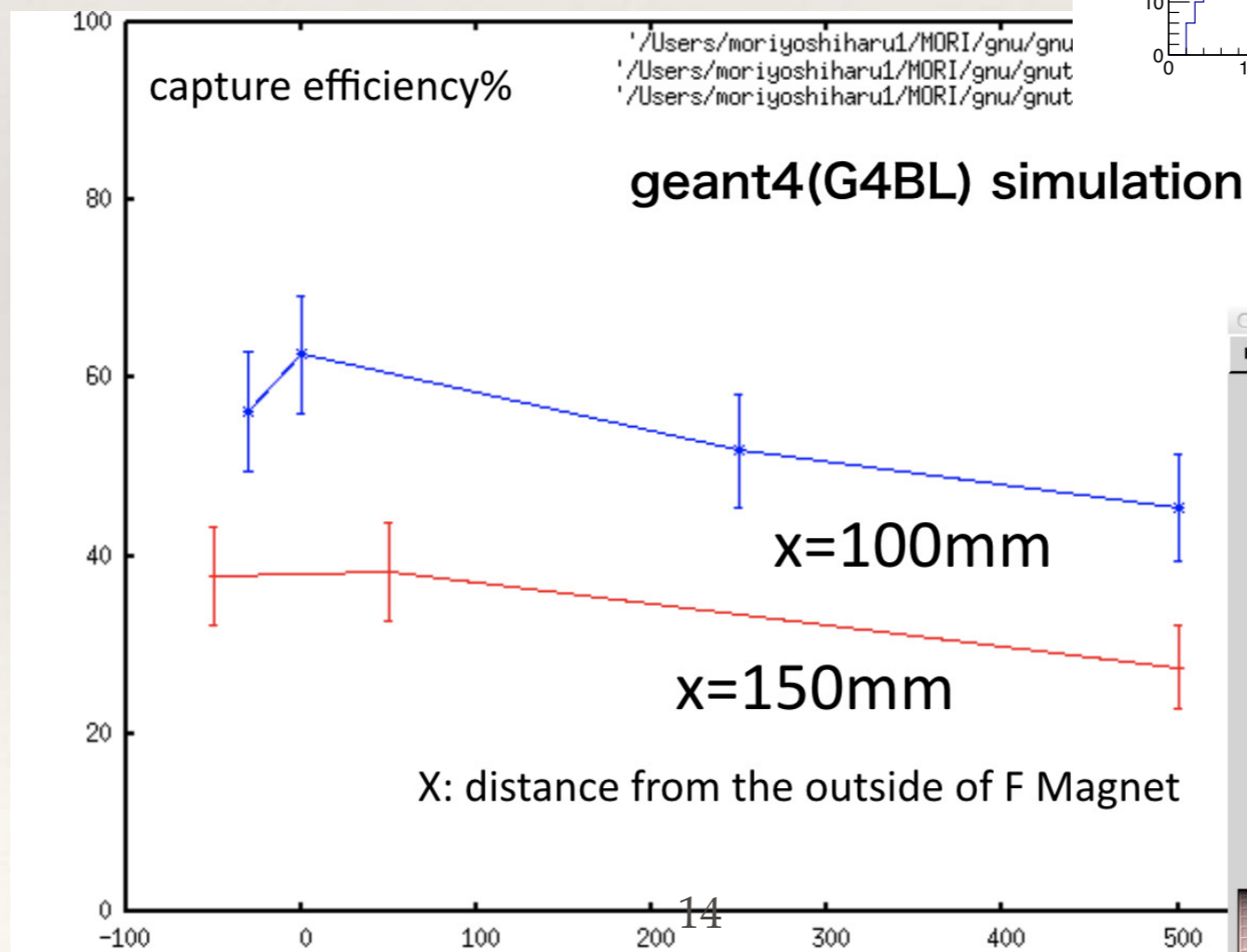
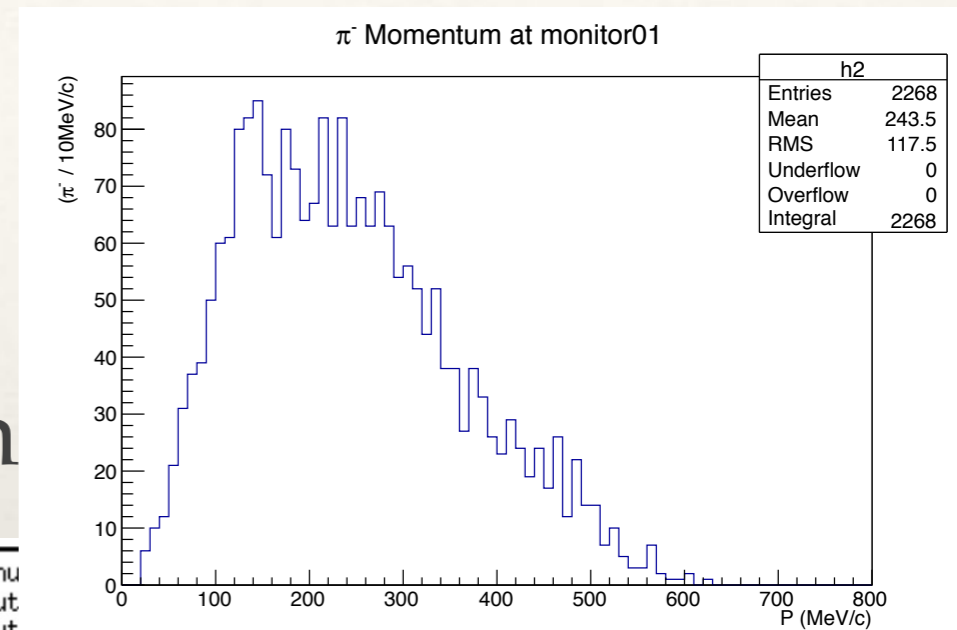
- ❖ Beam blow-up : ionization cooling
 - ❖ Suppressed for 3-D directions
 - ❖ horizontal: 6×10^{-4} m.rad.
 - ❖ vertical: 7×10^{-4} mrad.
 - ❖ Longitudinal: 3×10^{-3} eV.s

Well below dynamic apertures



MERIT : π/μ production ring(3)

- ❖ Capture and transport (π/μ)
- ❖ F-magnet and Solenoid (2T)
- ❖ Efficiency $\sim 50\%$: G4BL simulation



MERIT: Demonstration(1)

❖ Modify the ERIT 11MeV ring → 'MERIT-POP' ring : Nucl. Instrum. Method, A953 (2019)

❖ Acceleration

❖ Serpentine path acceleration

❖ $k=2.5 \rightarrow 0.07$: **modifying the magnet poles**

❖ 11MeV(fix) → **9.5 - 12MeV**

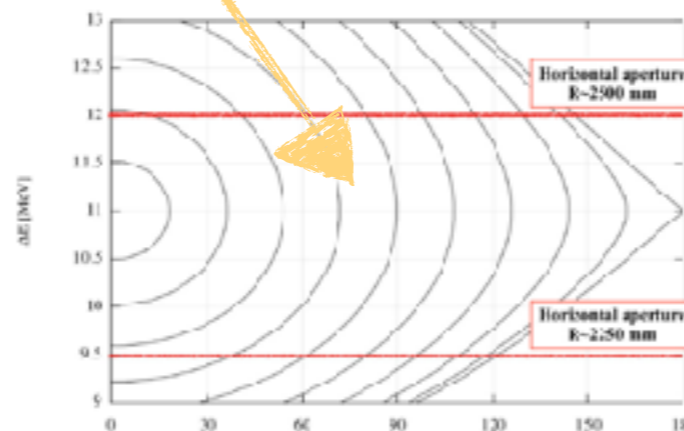
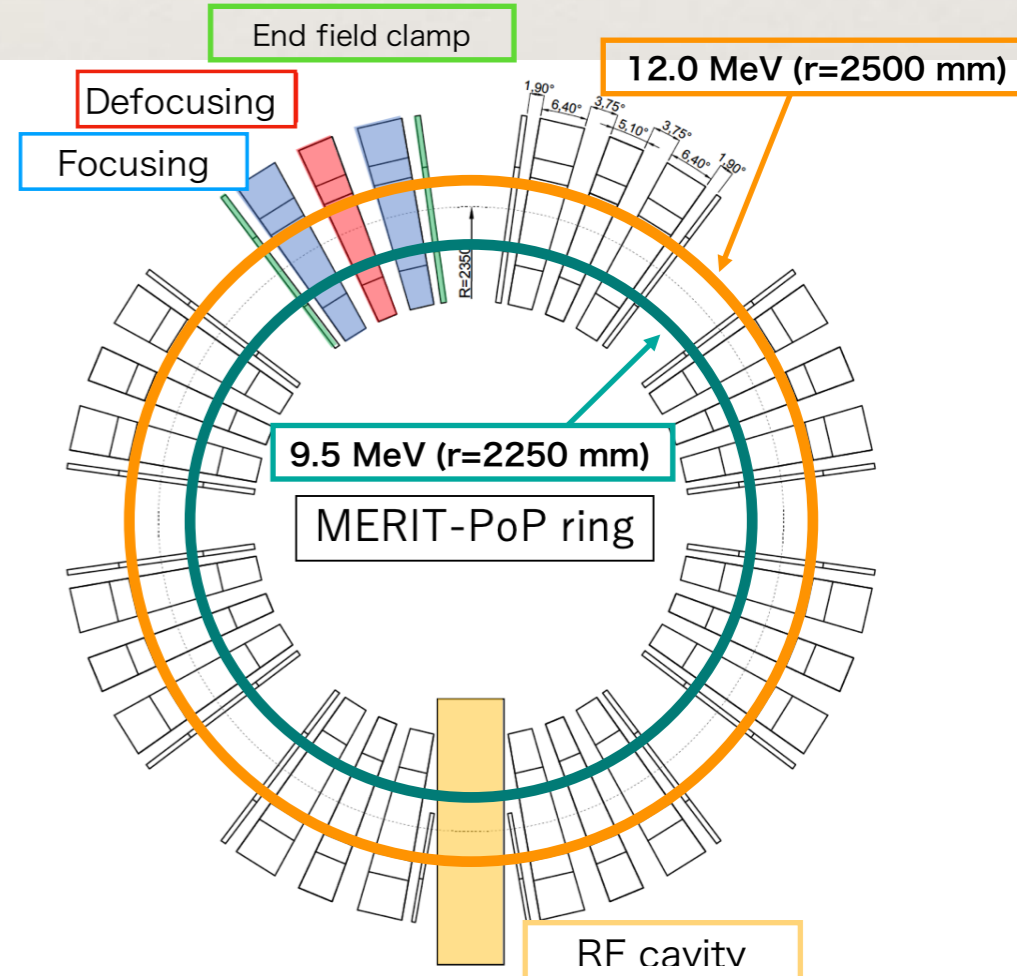
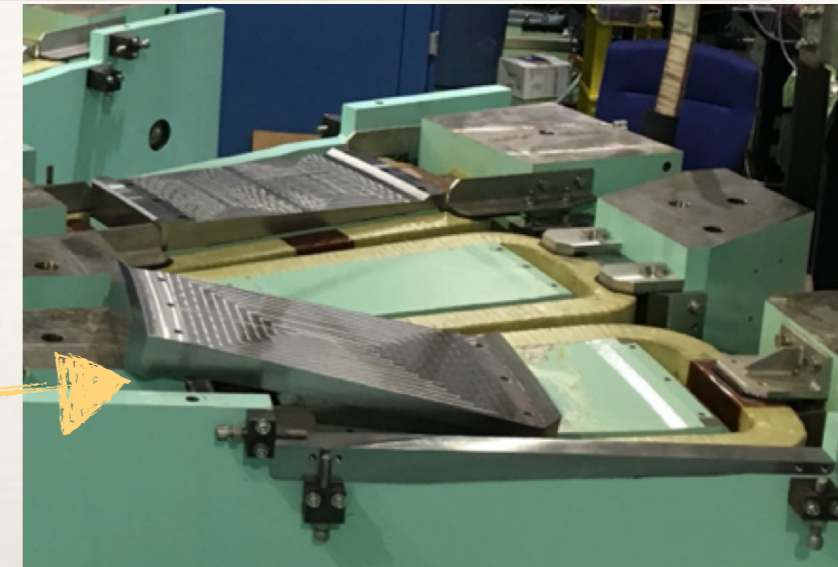
❖ **Close to integer resonance:**

$$\eta = \frac{1}{k+1} - \frac{1}{\gamma^2} \approx -0.044$$

$$Q_H \sim \sqrt{k+1} = 1.03$$

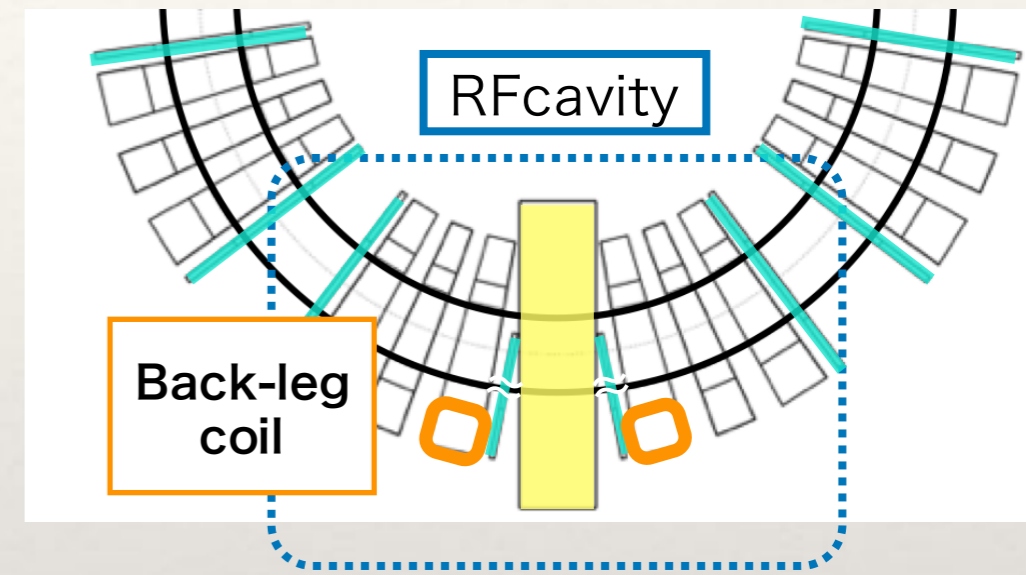
Parameters of MERIT-PoP ring.

Particle	Proton
Number of cells	8
Lattice	FDF-triplet
Field index k	0.07
Energy range [MeV]	9.5 - 12.0
Orbit radius [mm]	2250 - 2500
Slippage factor η	0.044
tune H/V	1.03/1.25
Parameters of F/D magnet	
Magnetic field [T]	0.59/0.14 (at $r = 2350$ [mm])
Opening angle of magnet [deg.]	5.1/6.4
Minimum half pole gap [mm]	84.0/85.2
Parameters of RF cavity	
RF voltage [kV]	75 - 225
Harmonic number	6
RF Frequency [MHz]	18.12

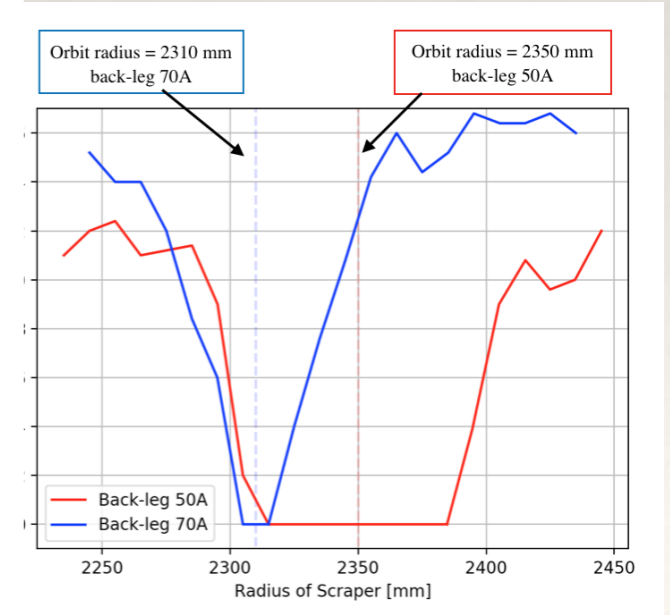
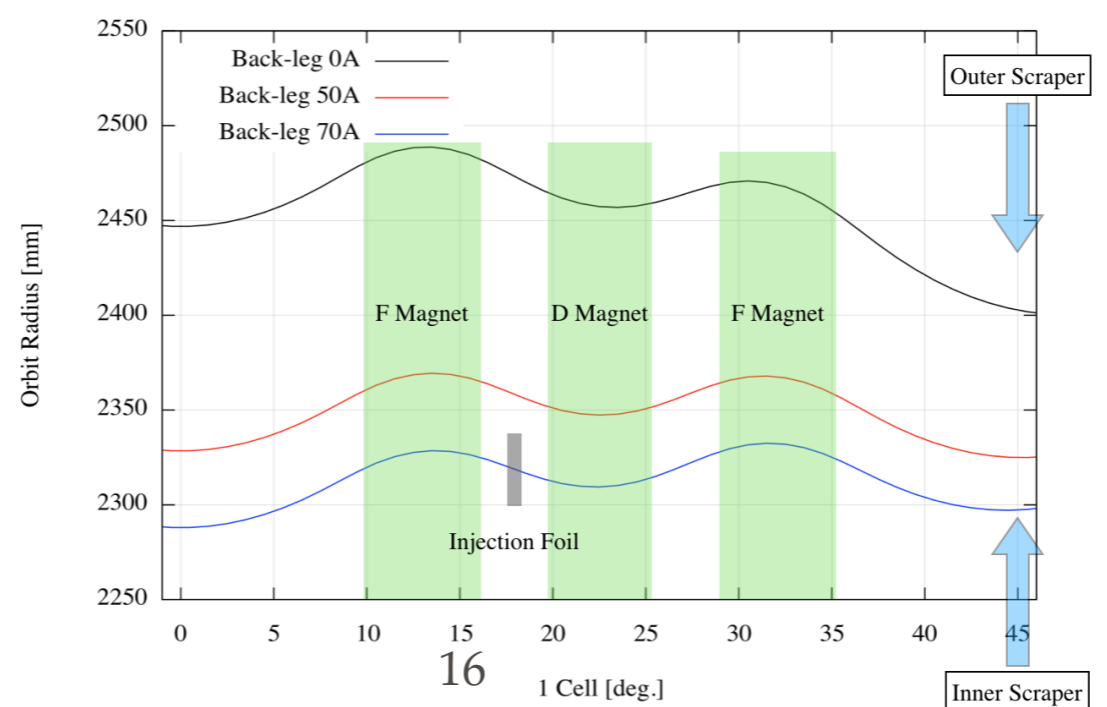
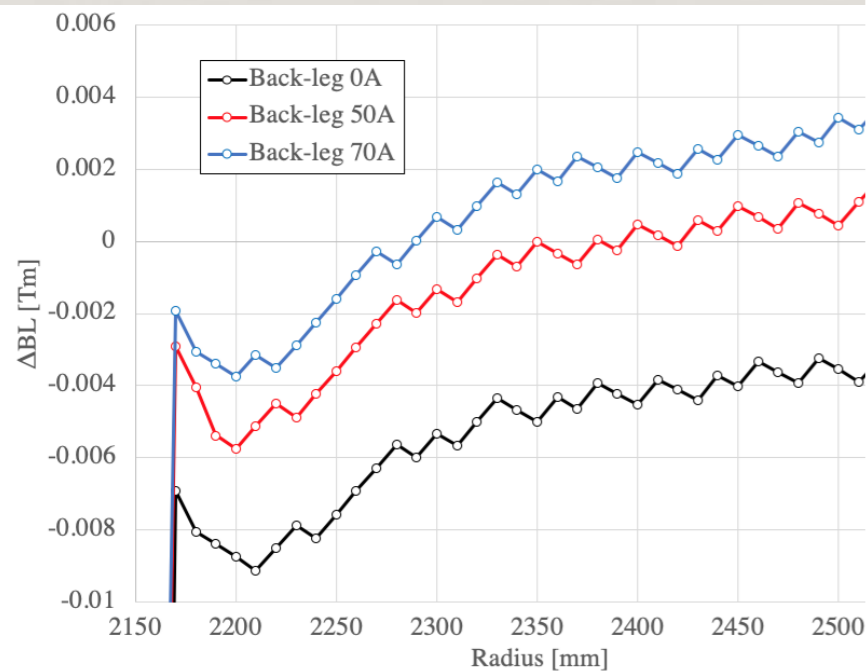


MERIT: Demonstration(2)

- ❖ Orbit correction
 - ❖ COD source : RF cavity (made of copper plating iron)
- ❖ COD correction and injection matching
 - ❖ A pair of back-leg coils wound around the magnet yokes



$$x(s) = \left[\frac{\sqrt{\beta(s)\beta(s_0)} \delta(Bl)}{2 \sin(\pi\nu_H) B\rho} \right] \cos(\pi\nu_H - |\psi(s) - \psi(s_0)|)$$



MERIT: Demonstration(3)

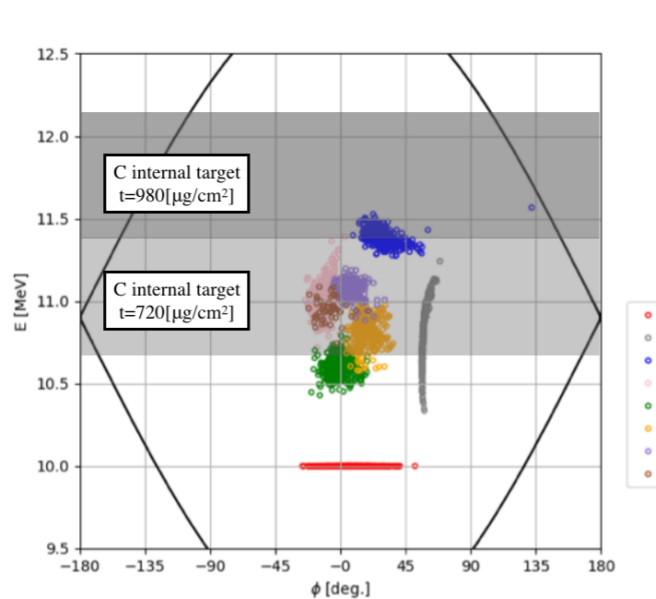
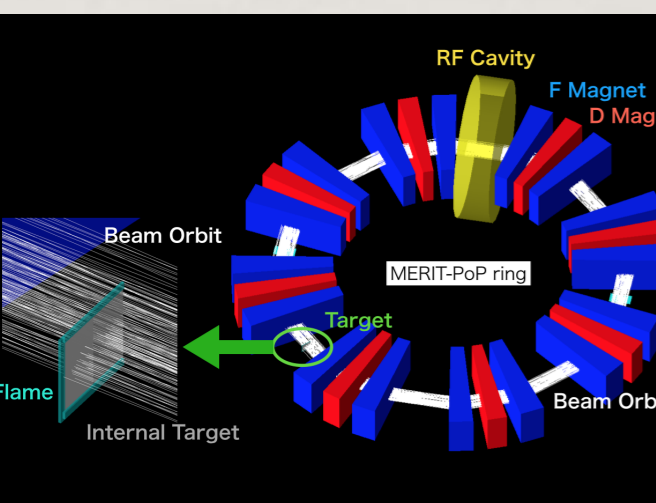
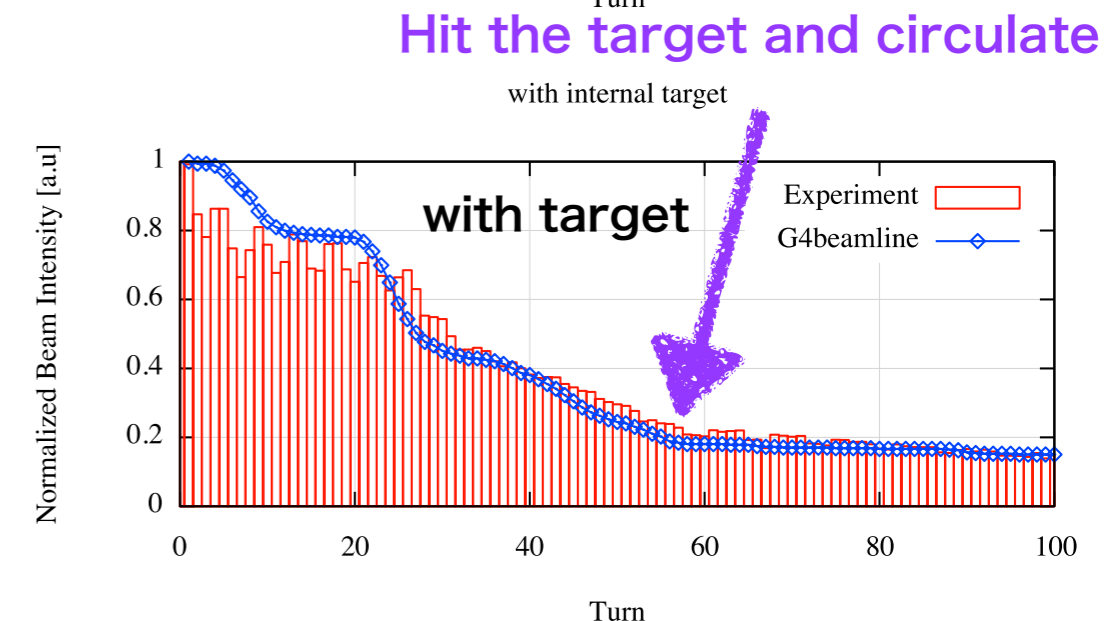
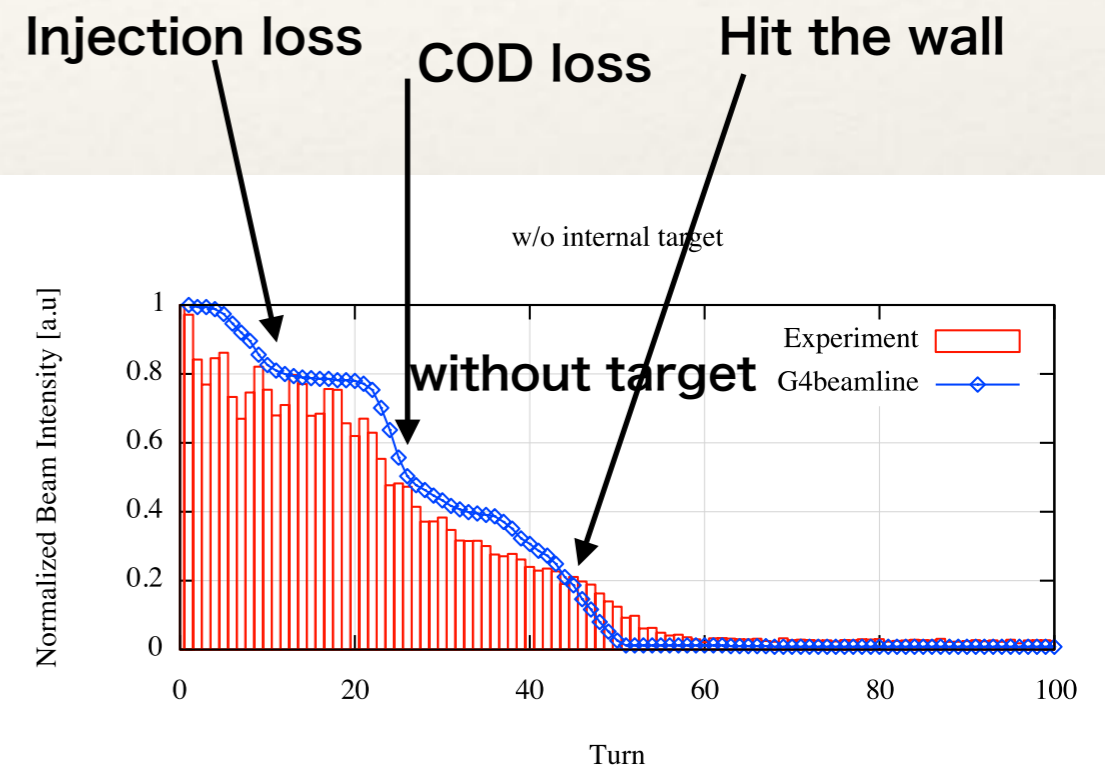
❖ Experiment

- ❖ Wedge target: C, $t=720-980[\text{g}/\text{cm}^2] \rightarrow \Delta E=27-37\text{keV}$

❖ Particle tracking

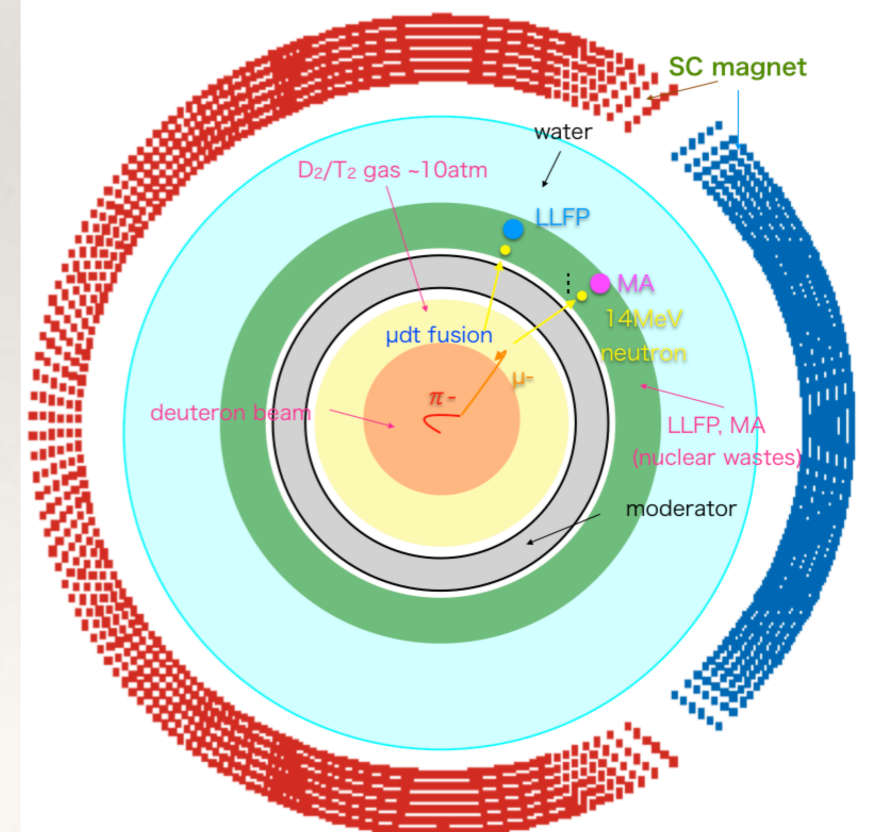
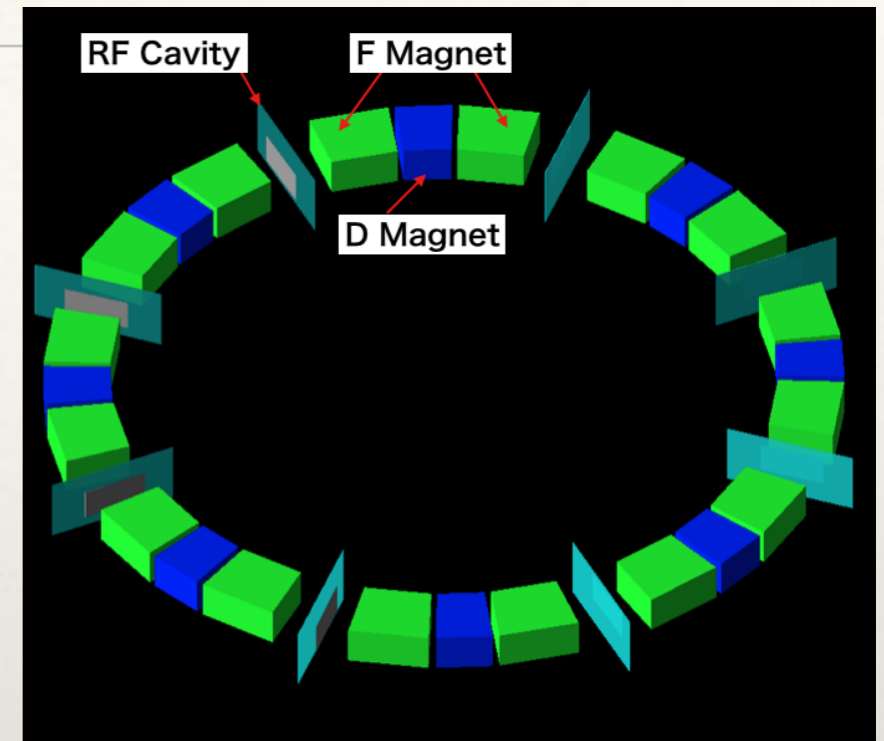
- ❖ G4beamline(G4BL) code
- ❖ B-Field map 3D: OPERA3D/TOSCA

❖ Experiments and simulations showed good agreement.



NX: Hybrid of MuCF and ERIT (1)

- ❖ Advances of ERIT for nuclear transmutation
 - ❖ Hybrid system of MuCF and ERIT
 - ❖ D/T gas target $\sim 1-10\text{atm}$
 - ❖ Neutron flux $\phi(n): 10^{19}\text{n/s}$
 - ❖ Muon flux required: $\phi(\mu^-) = 7 \times 10^{16} \mu / \text{s}$
 - ❖ d beam : $400\text{MeV/u} - 60\text{mA}$ ($50\text{MW} : \text{D}^0$ incident)
 - ❖ [Nucl. Instrum. Method, A982 (2019)]
 - ❖ Electric power required : $<10\%$ of 1GWe nuclear plant generating capacity
 - ❖ MuCF fusion output power ($\sim 20\text{MW}$) assists.



NX: Hybrid of MuCF and ERIT(2)

- ❖ Gas filling ERIT

- ❖ D2 gas, 1atm

- ❖ Emittance growth

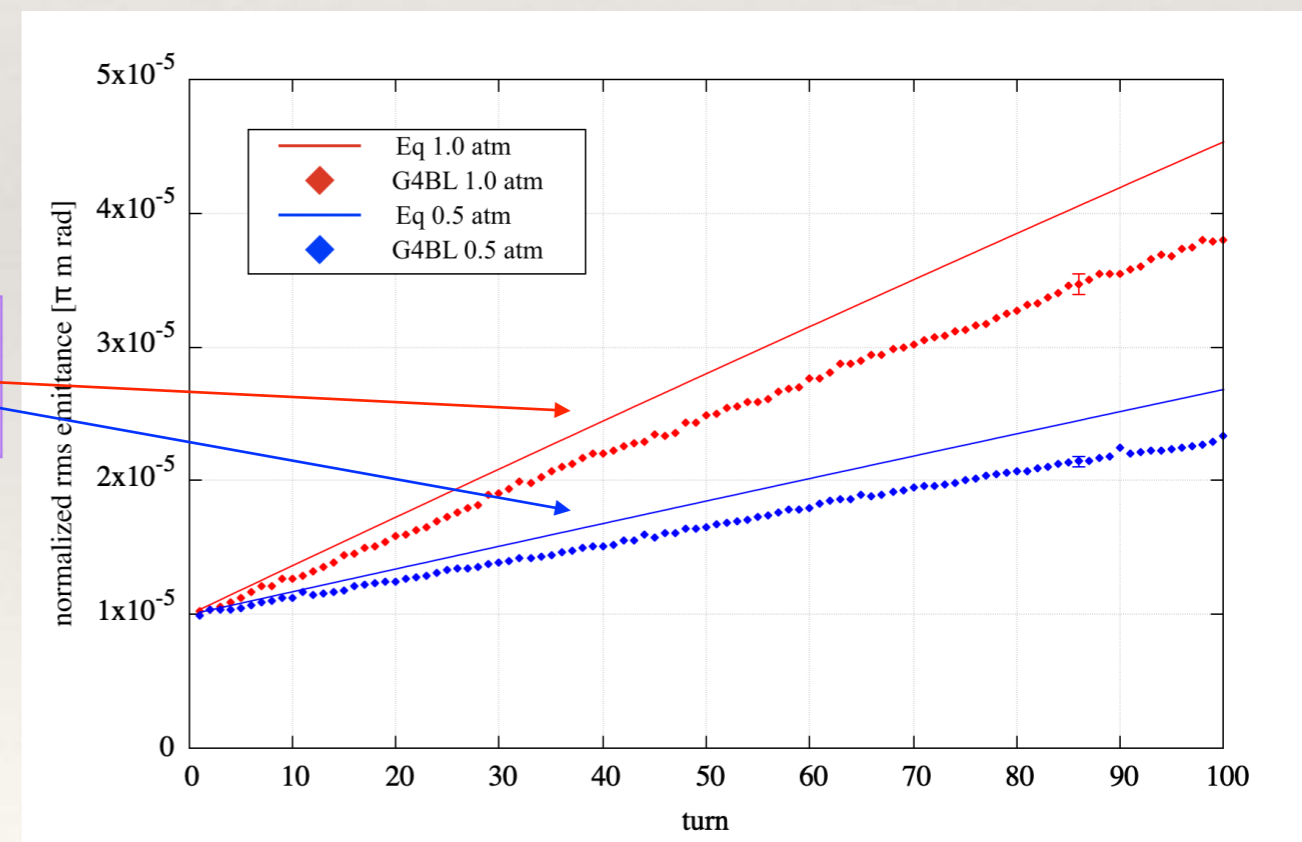
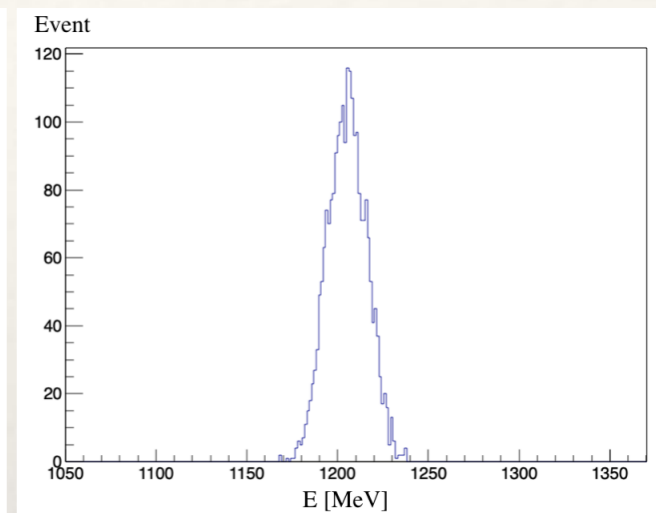
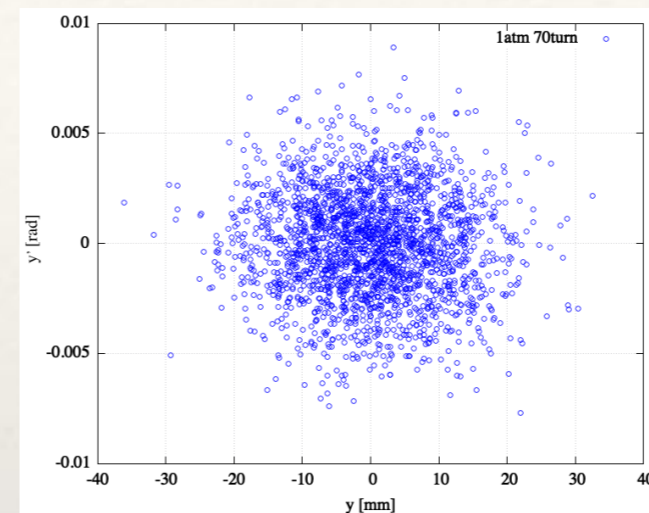
- ❖ Longitudinal : $\Delta E / E \sim 2.5\%$ (FWHM)

- ❖ Transverse: $3 \times 10^{-5} \text{m.rad}$ after 70 turns.

$$\frac{d\epsilon_N}{ds} = -\frac{1}{\beta^2 E} \frac{dE}{ds} \epsilon_N + \frac{\beta\gamma\beta_T}{2} \frac{d\langle \theta_{rms}^2 \rangle}{ds}$$

- ❖ Acceptance

- ❖ Energy acceptance : $> \pm 10\%$
 - ❖ Transverse: $4 \times 10^{-3} \text{m.rad}$



Summary

- ❖ Applications of Energy Recovery Internal Target(ERIT) with FFA accelerator
 - ❖ Mitigation of long-lived nuclear wastes with negative muons
 - ❖ Neutron source : Muon Catalyzed Fusion
 - ❖ Direct nuclear transmutation : Muonic atom
- ❖ MERIT :a new scheme that achieves acceleration and circulation.
 - ❖ Design of negative muon source with MERIT
 - ❖ Demonstration of MERIT principle
- ❖ Hybrid system for NX: MuCF and ERIT