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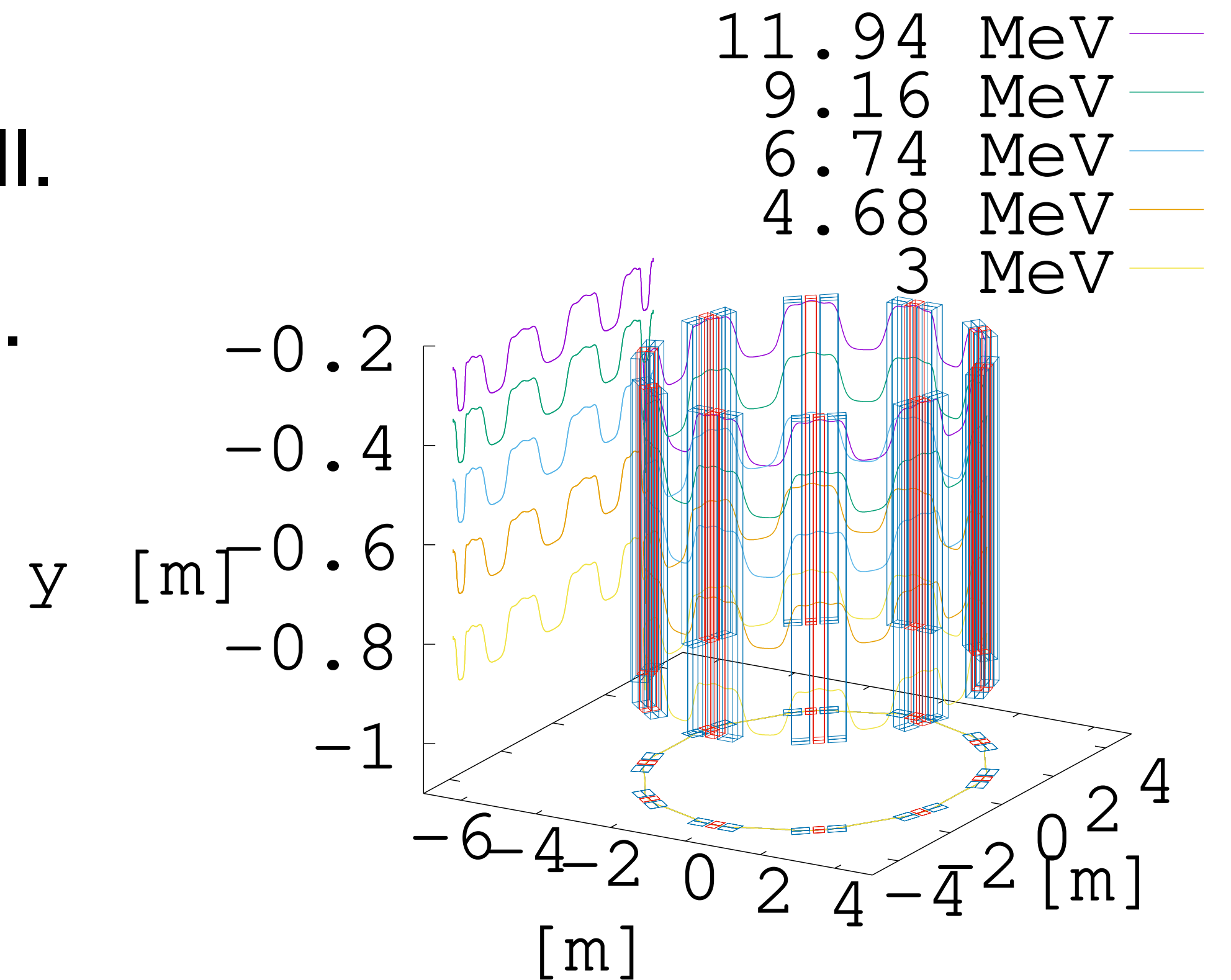
Beam Stacking in a Vertical FFA

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FFA'20 Workshop, TRIUMF (Nov 30th - Dec 4th, 2020)

Introduction

- The FETS-FFA is a prototype ring for ISIS-II.
- Demonstrating beam stacking is a key aim.
 - Allows flexibility in the delivery of beam to target stations.
 - Allows lower repetition rates at high peak output.



Beam stacking

- Successive beam pulses are stored in the ring. Coasting beams are stacked in terms of energy (in a VFFA they are also stacked vertically!).
- What is the effect of the accelerating RF on the stacked beam? The topic was first addressed by K. Symon and A. Sessler.



Phase Displacement

Scattering

Subharmonic effects



Effect of RF on the stacked beam

Phase Displacement

- Accelerating bucket will cause a downward shift in the energy of the coasting beam it moves through (a consequence of Liouville theorem)[^].

$$\langle E_{shift} \rangle = \frac{\omega_0 A}{2\pi}$$

Scattering

- The energy spread of the beam is increased by a bucket passing through. The effect is proportional to $\Gamma = \sin\phi_s$.

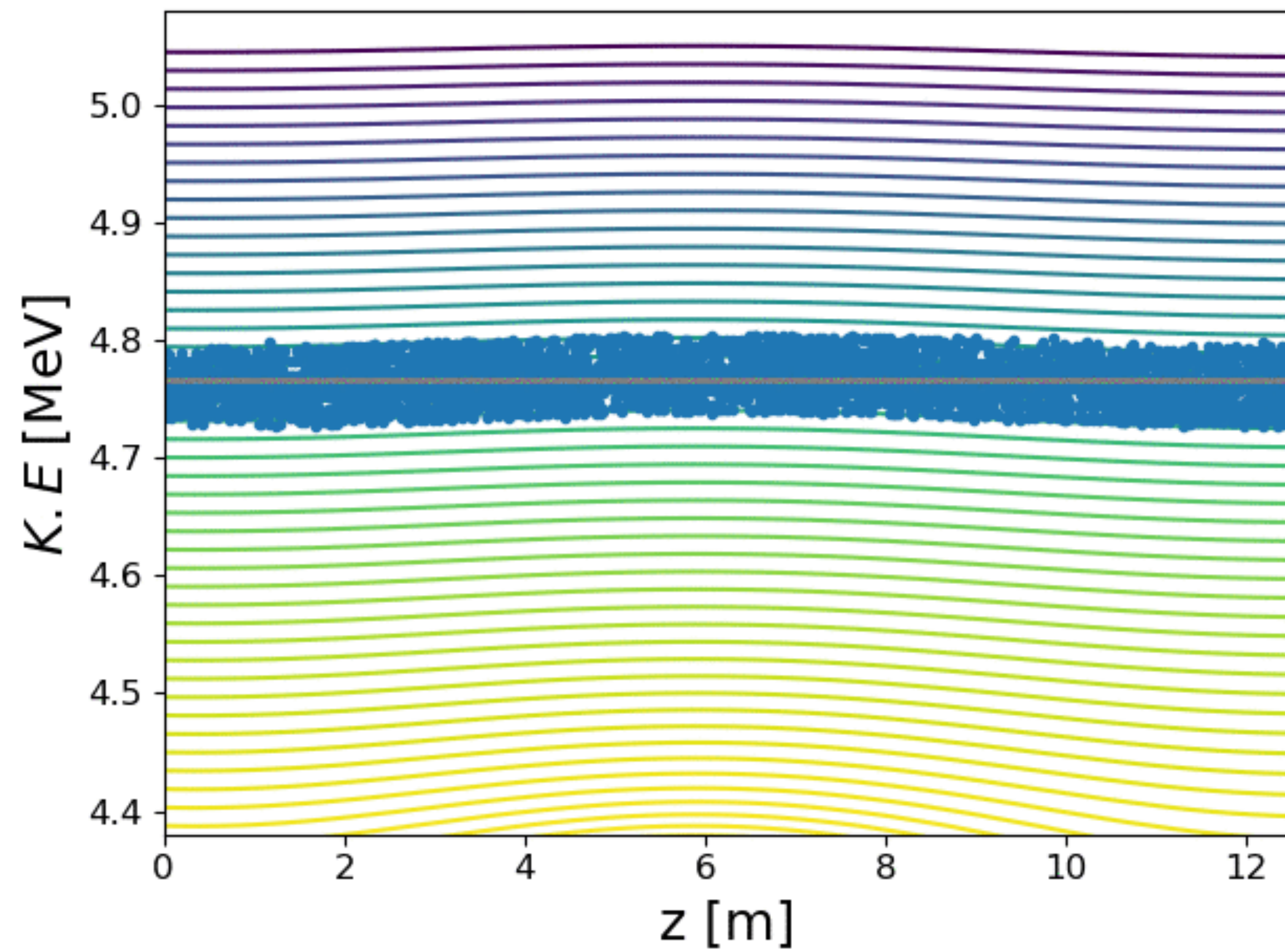
$$\sigma = \frac{16}{(2\pi)^{3/2}} \Gamma(\phi_s) \sqrt{\frac{eVE}{h|\eta|}}$$

Subharmonics

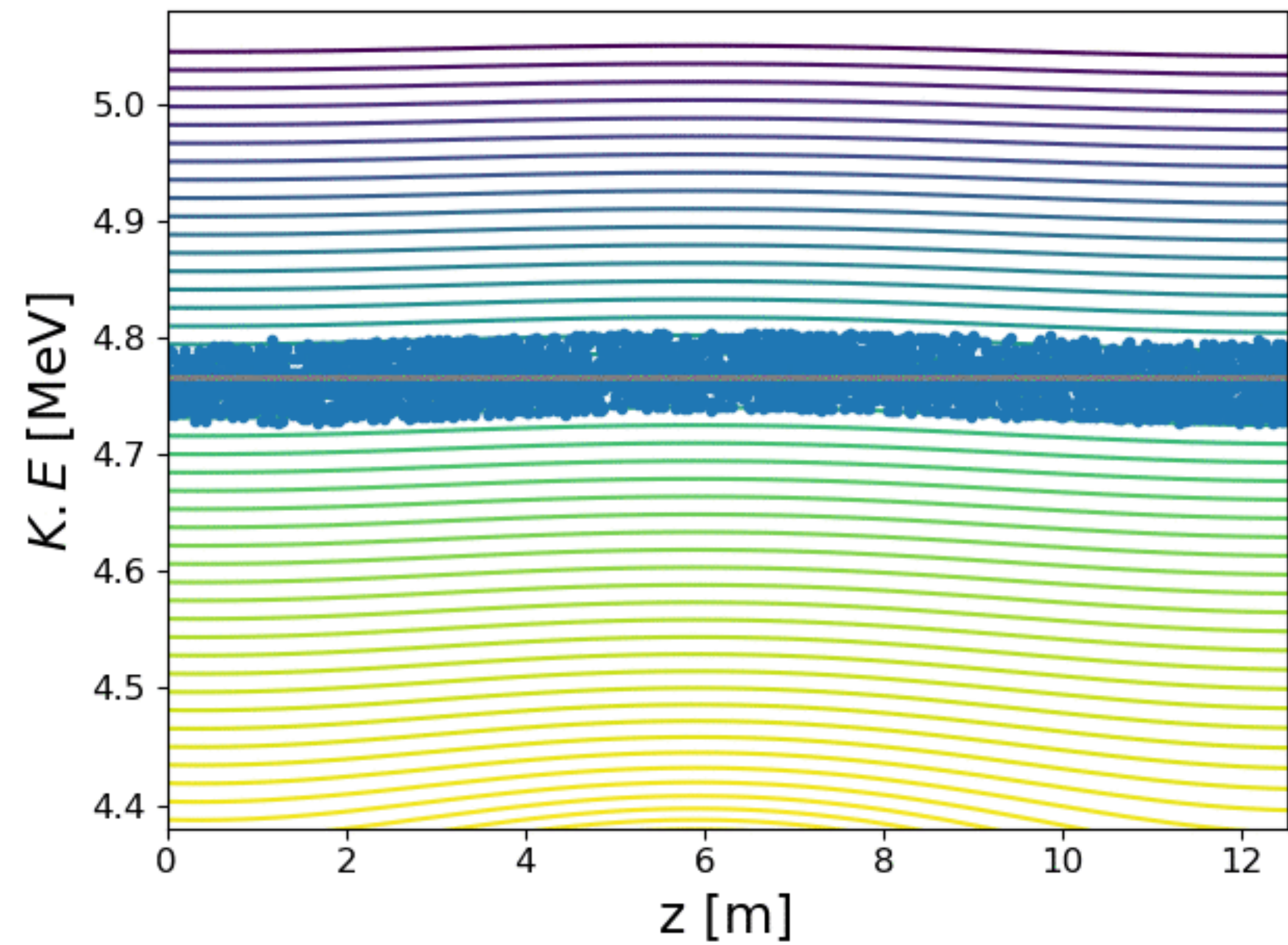
- If $f_{stack}/f_{rf} = m/n$ then the RF may affect the stacked beam. In the case of “bucket lift” some of the stacked beam is trapped and accelerated in a subharmonic bucket.

Movies

Empty bucket passing through a coasting beam



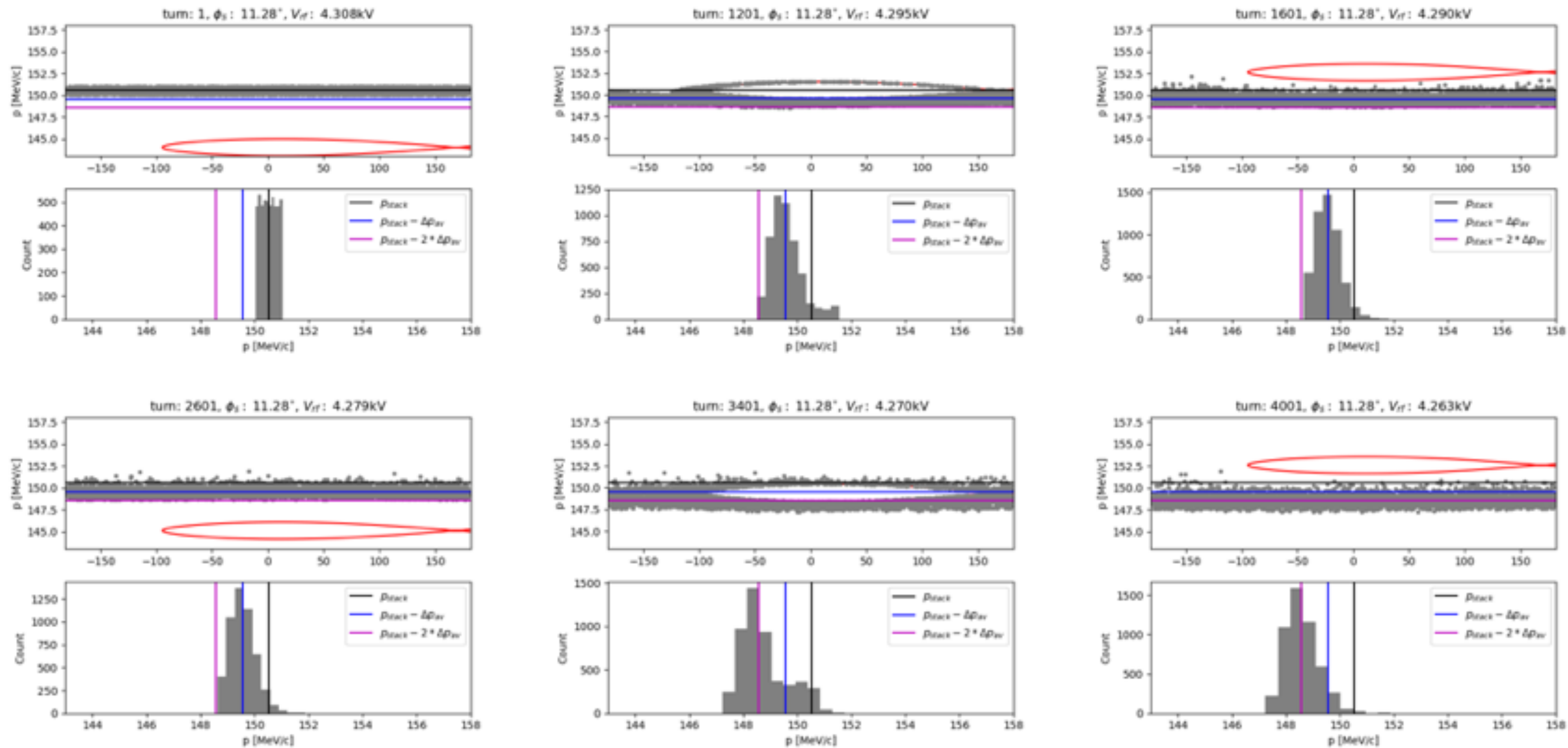
$$\phi_s = 5^\circ$$



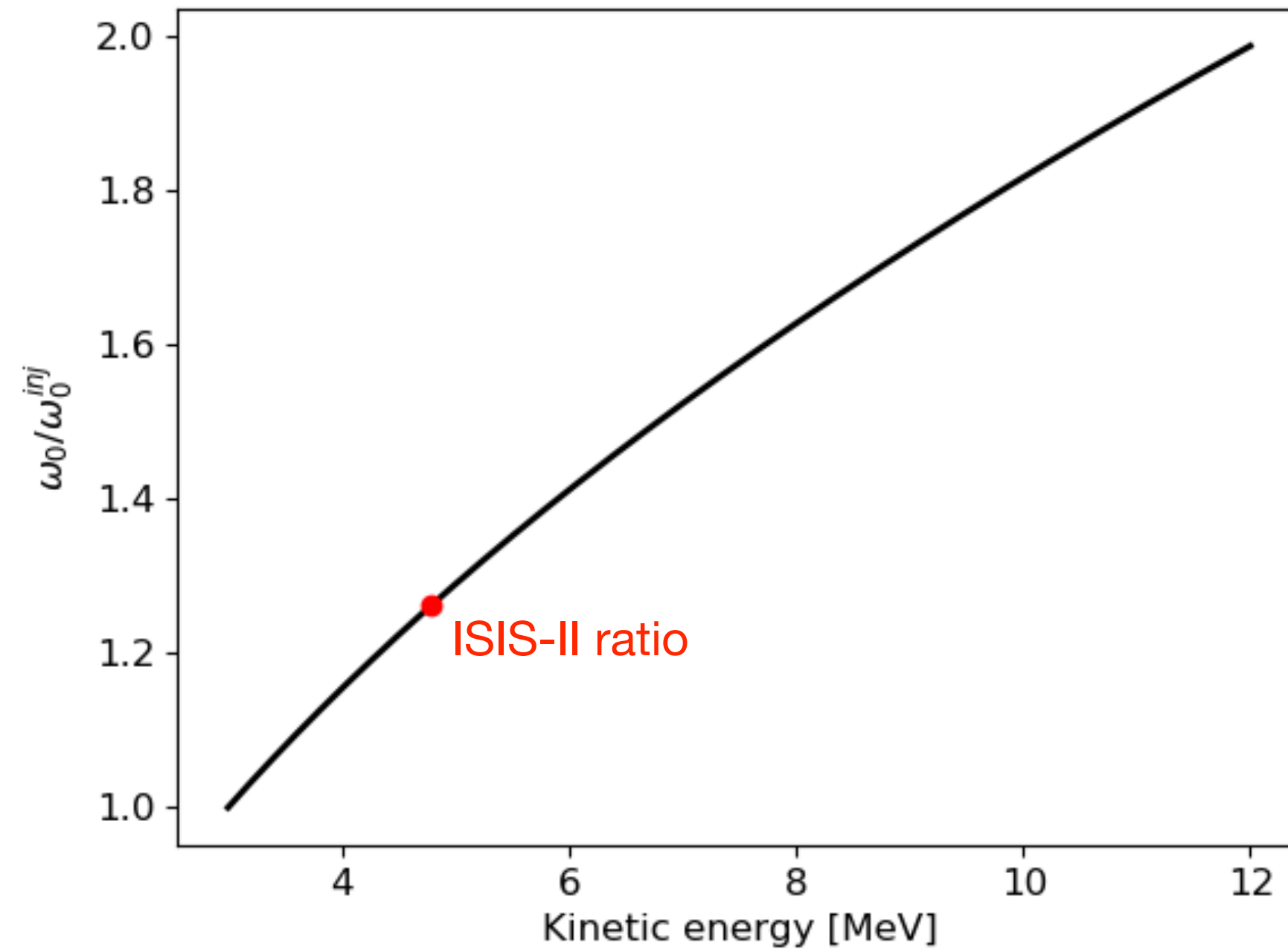
$$\phi_s = 10^\circ$$

Multiple bucket passes

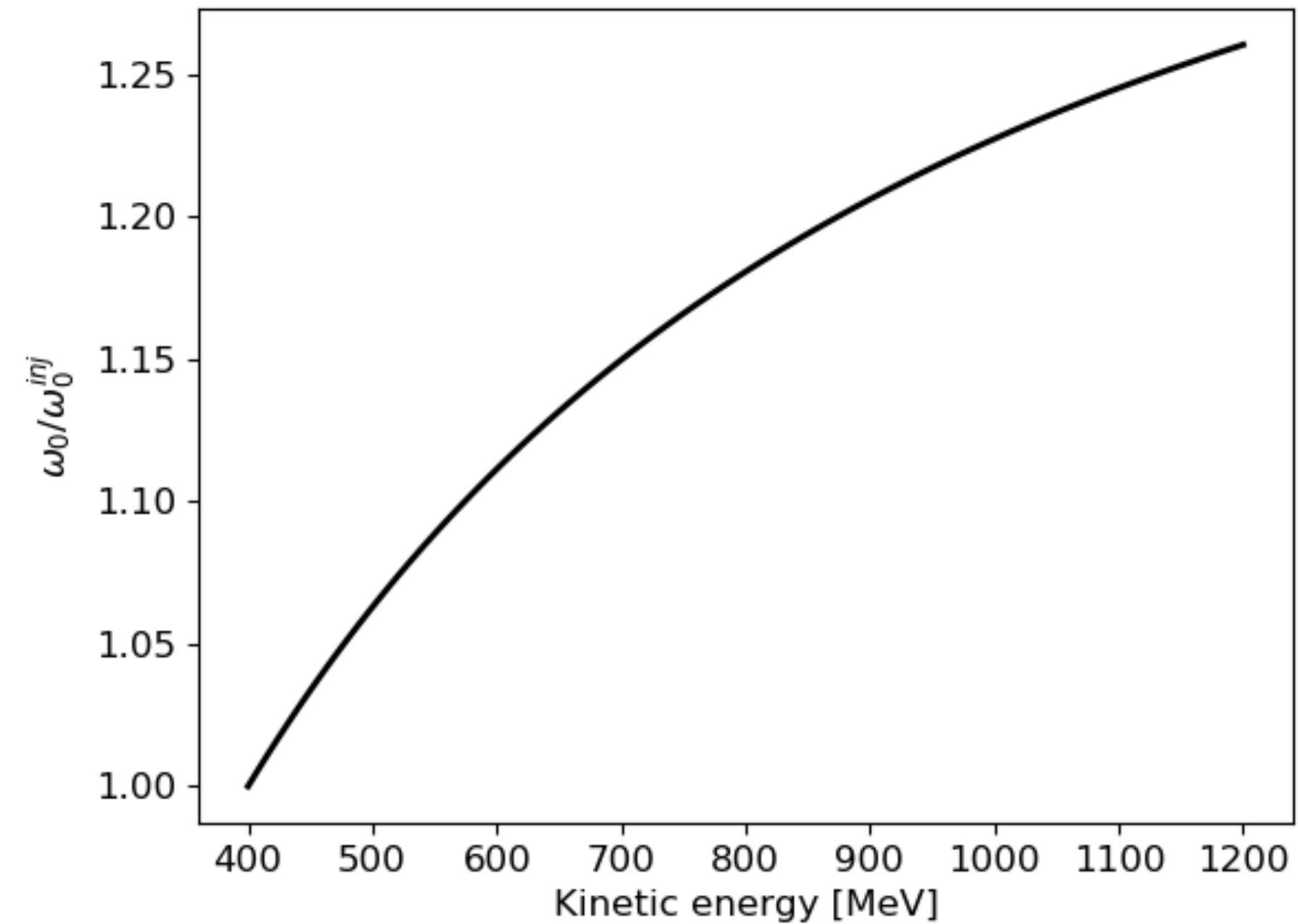
Empty buckets passing through coasting beam



Stacking energy choice



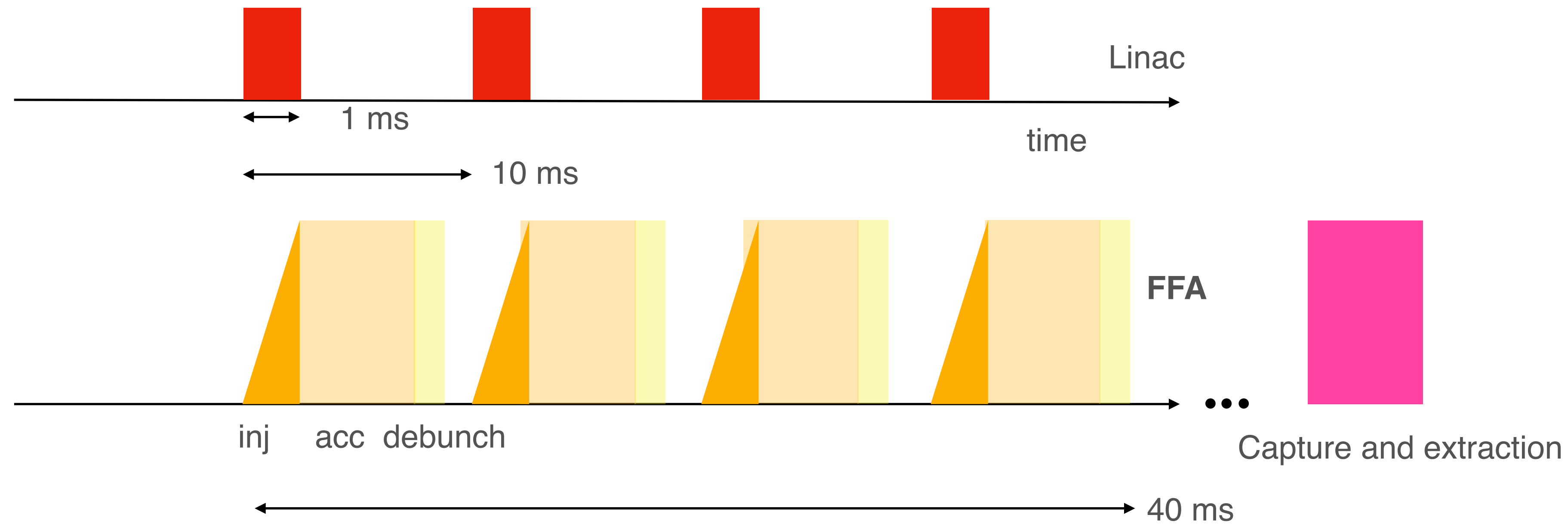
FETS-FFA



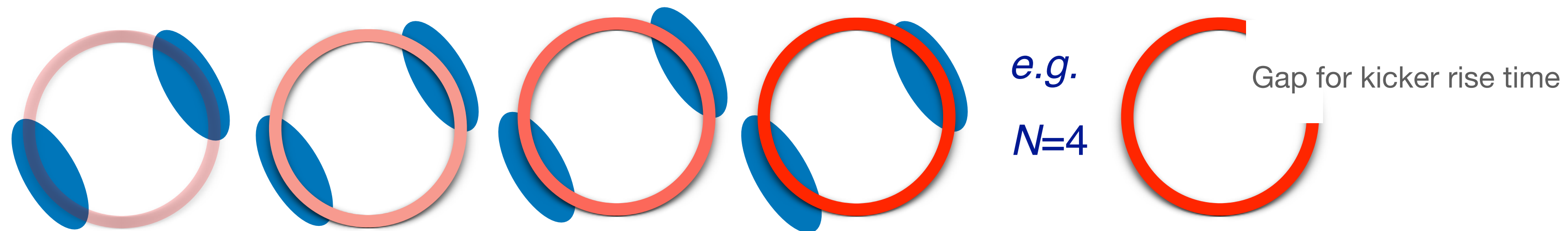
ISIS-II

- Avoid the stacked beam seeing harmonics of the RF during acceleration.
- A natural choice is 4.8MeV where the frequency ratio corresponds to ISIS-II.

Beam Stacking Scheme

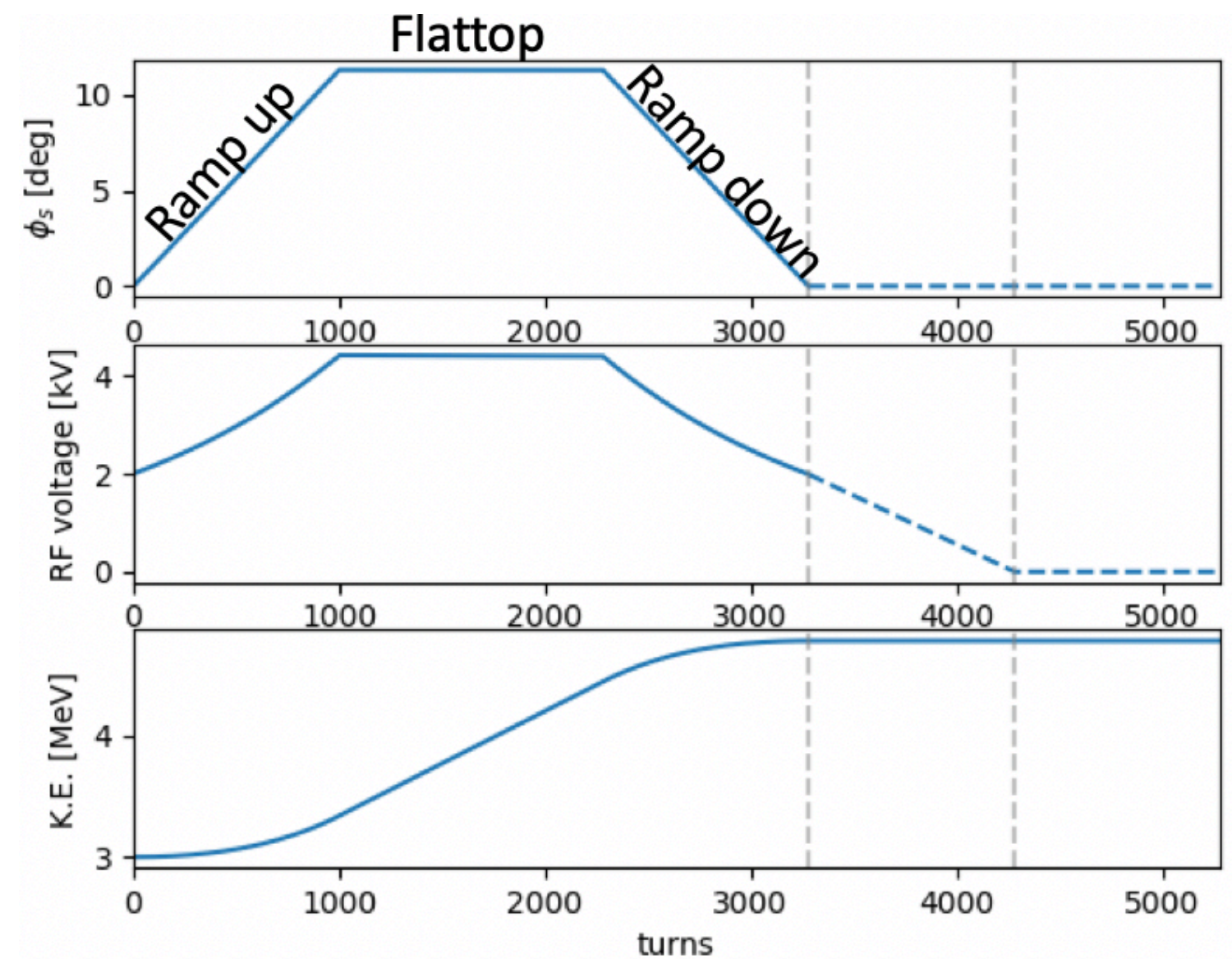


N	Rep rate
1	100 Hz
2	50 Hz
5	20 Hz
10	10 Hz



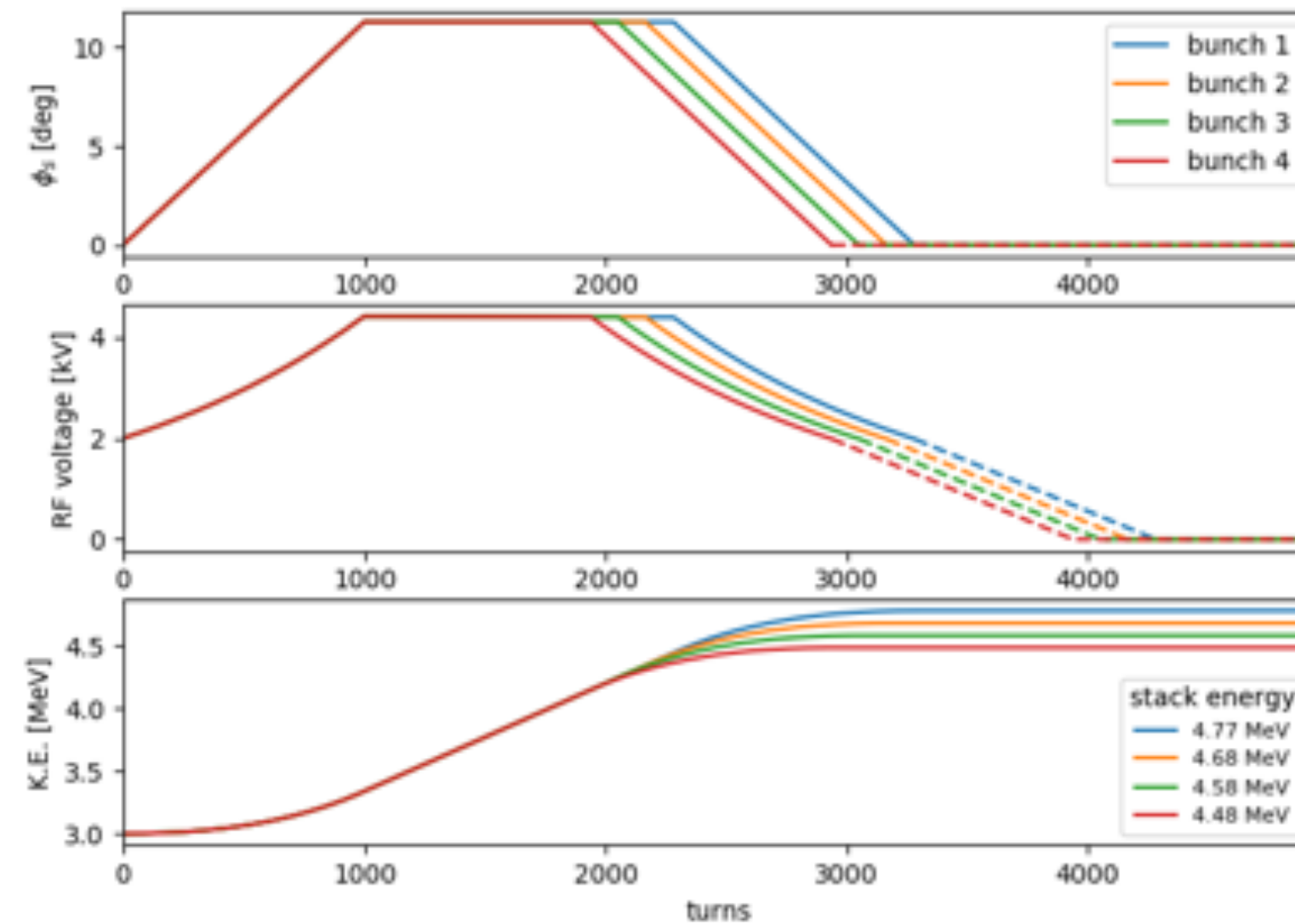
- Stack N beams to reduce the beam seen by users by a factor N .

FETS-FFA: Stacking at the bottom



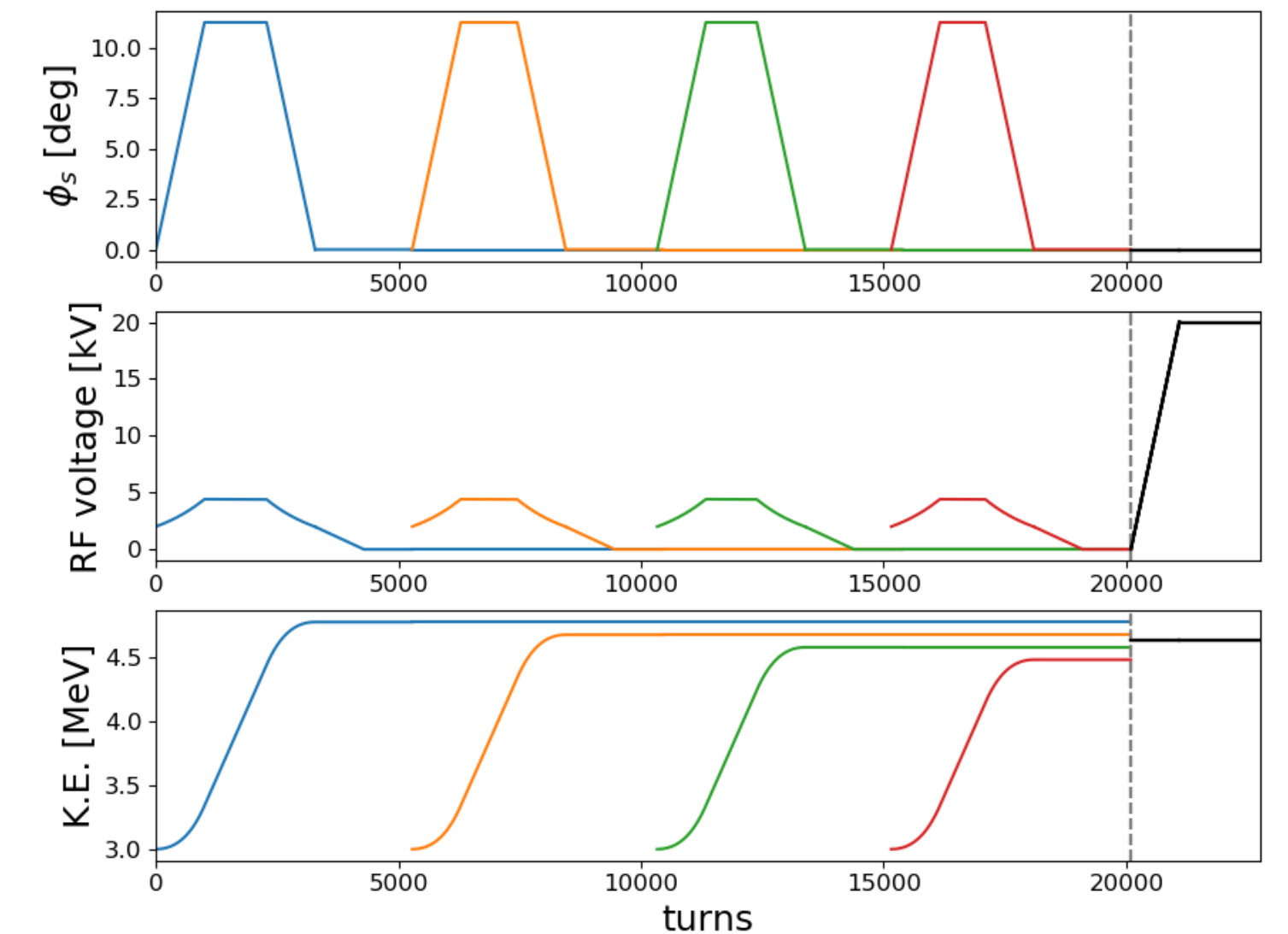
← Acceleration (constant bucket area)
 → Reduce bucket area
 → RF reset

Stacking a single beam



- Stack at the bottom by adjusting number of turns in flattop.
- This ensures the final energy of each consecutive is reduced by the phase displacement shift.

Stacking multiple beams (overlaid)

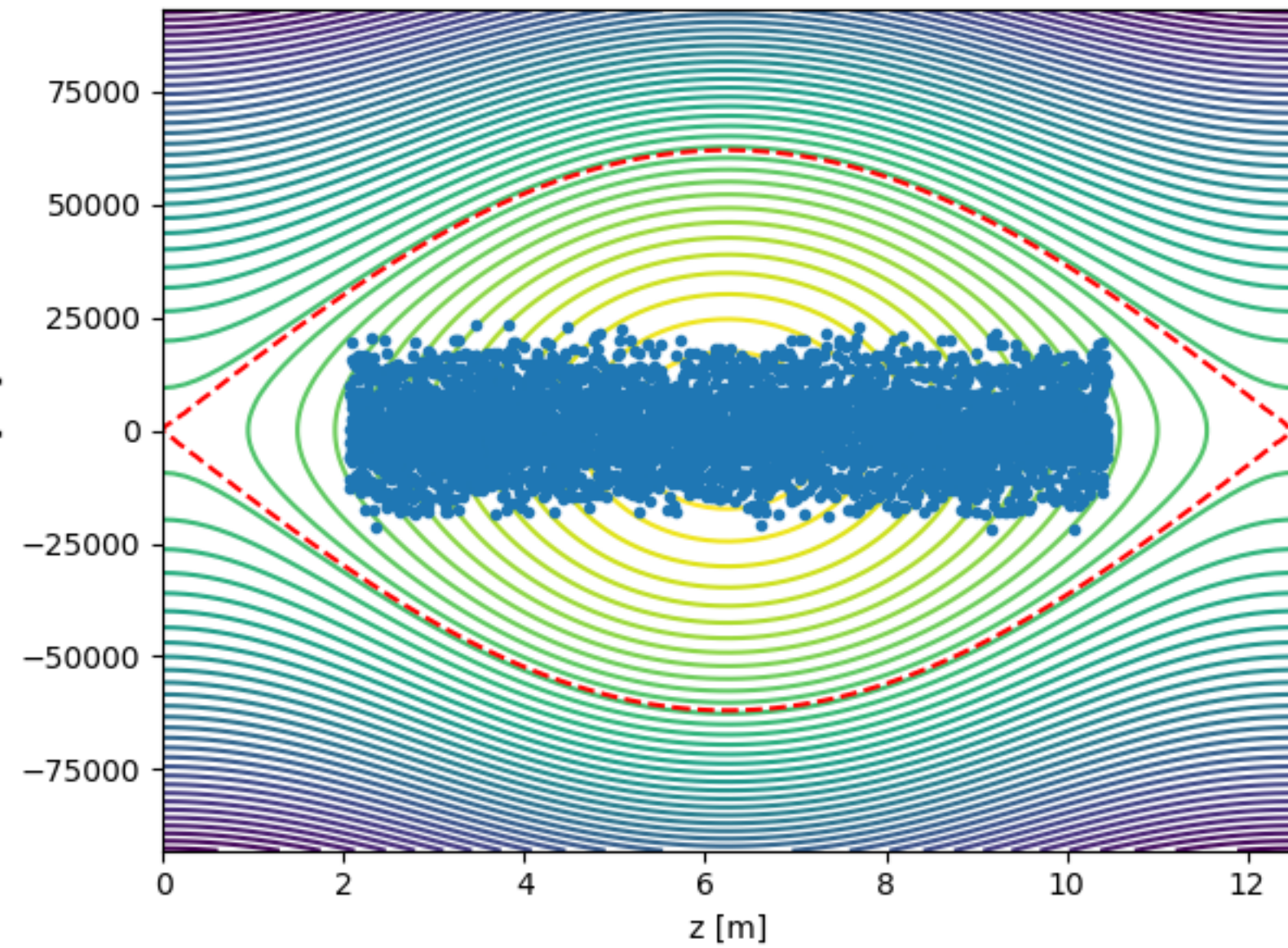


← Accelerate and stack four beams
 ← Capture

Stacking multiple beams (sequential)

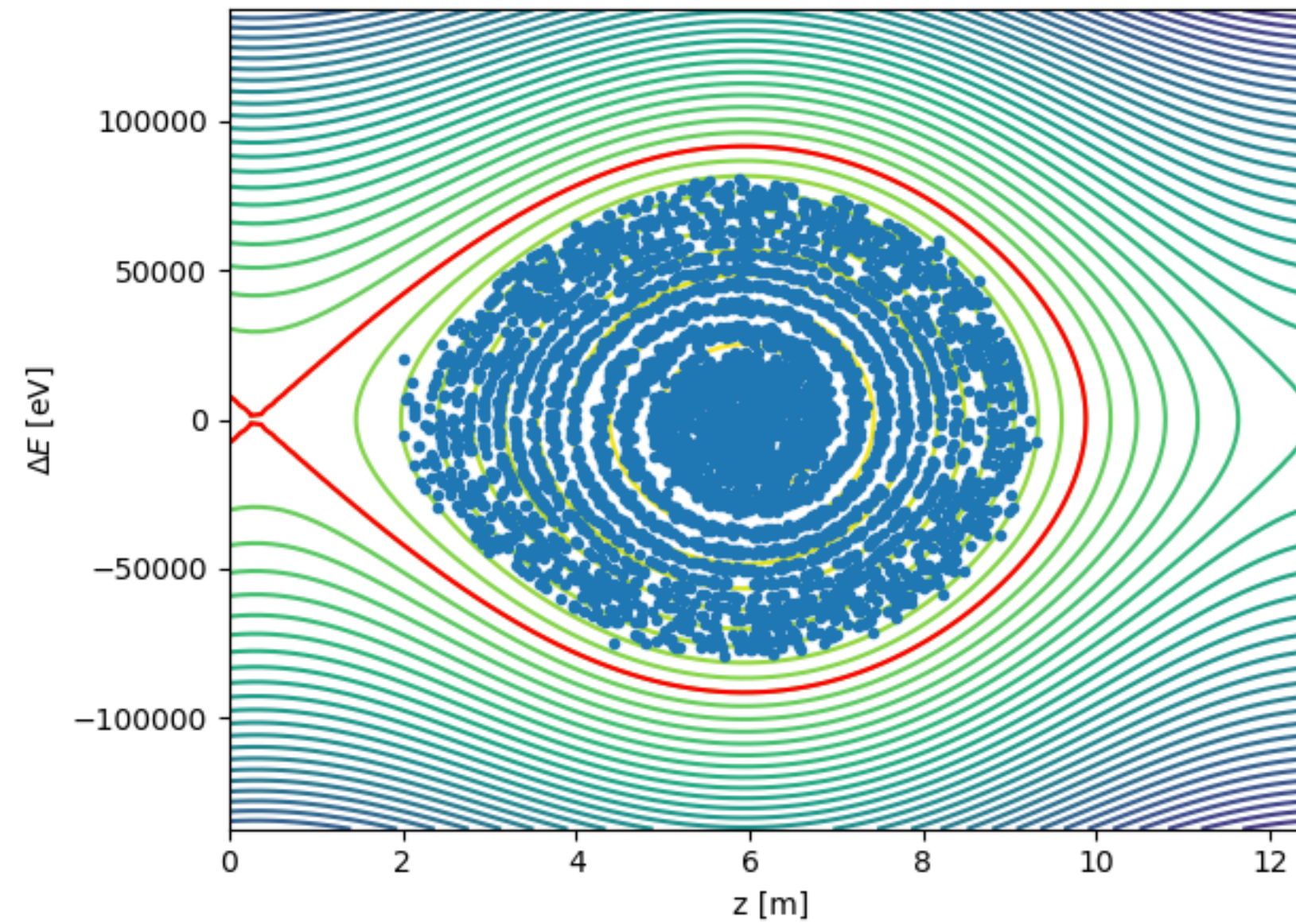
FETS-FFA: Acceleration stage

turn index 0 K.E. 3.000MeV V0 2.0 kV



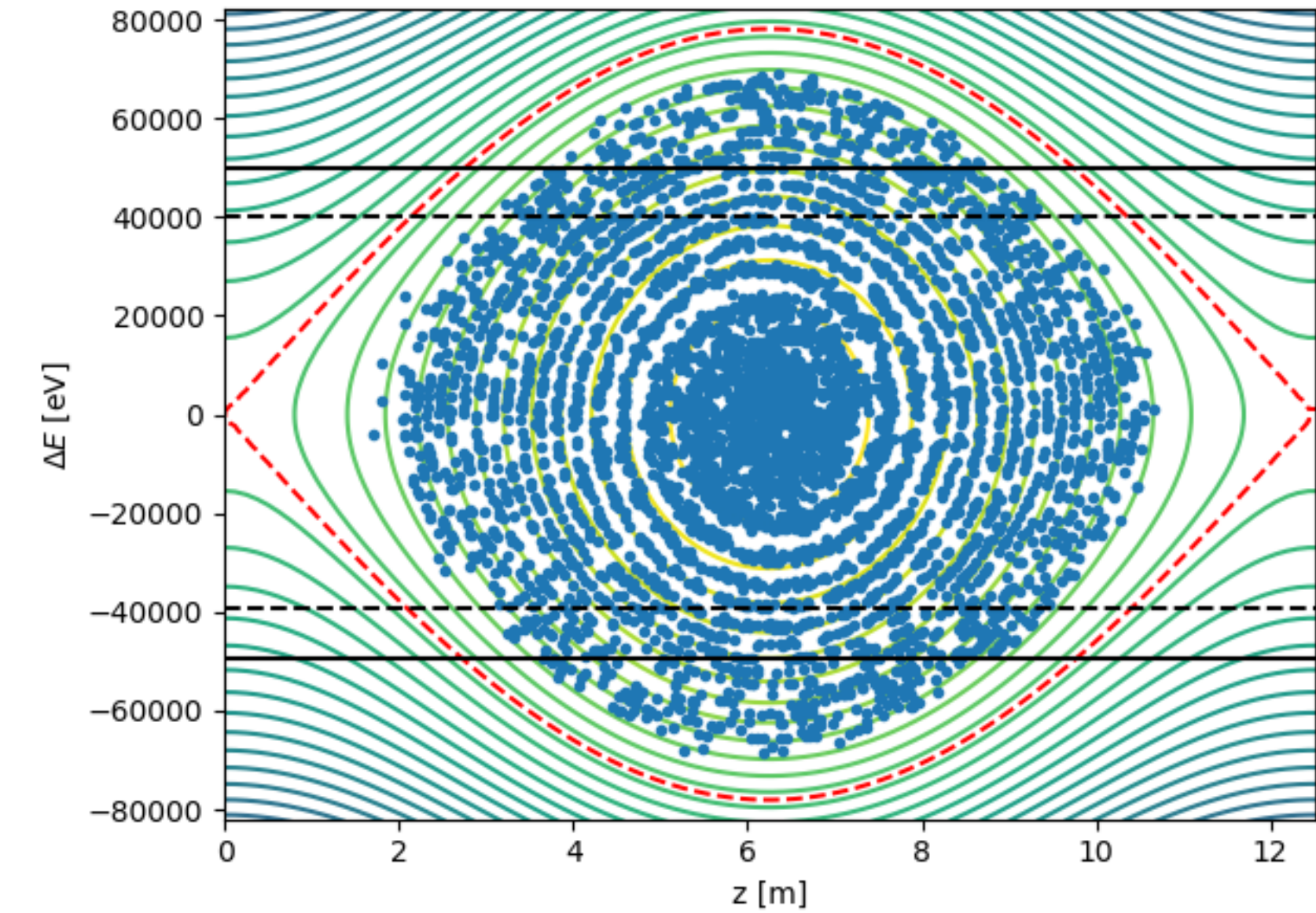
Injection ($\phi_s = 0$)

turn index 2500 K.E. 4.597MeV V0 3.692 kV



End of ϕ_s flattop

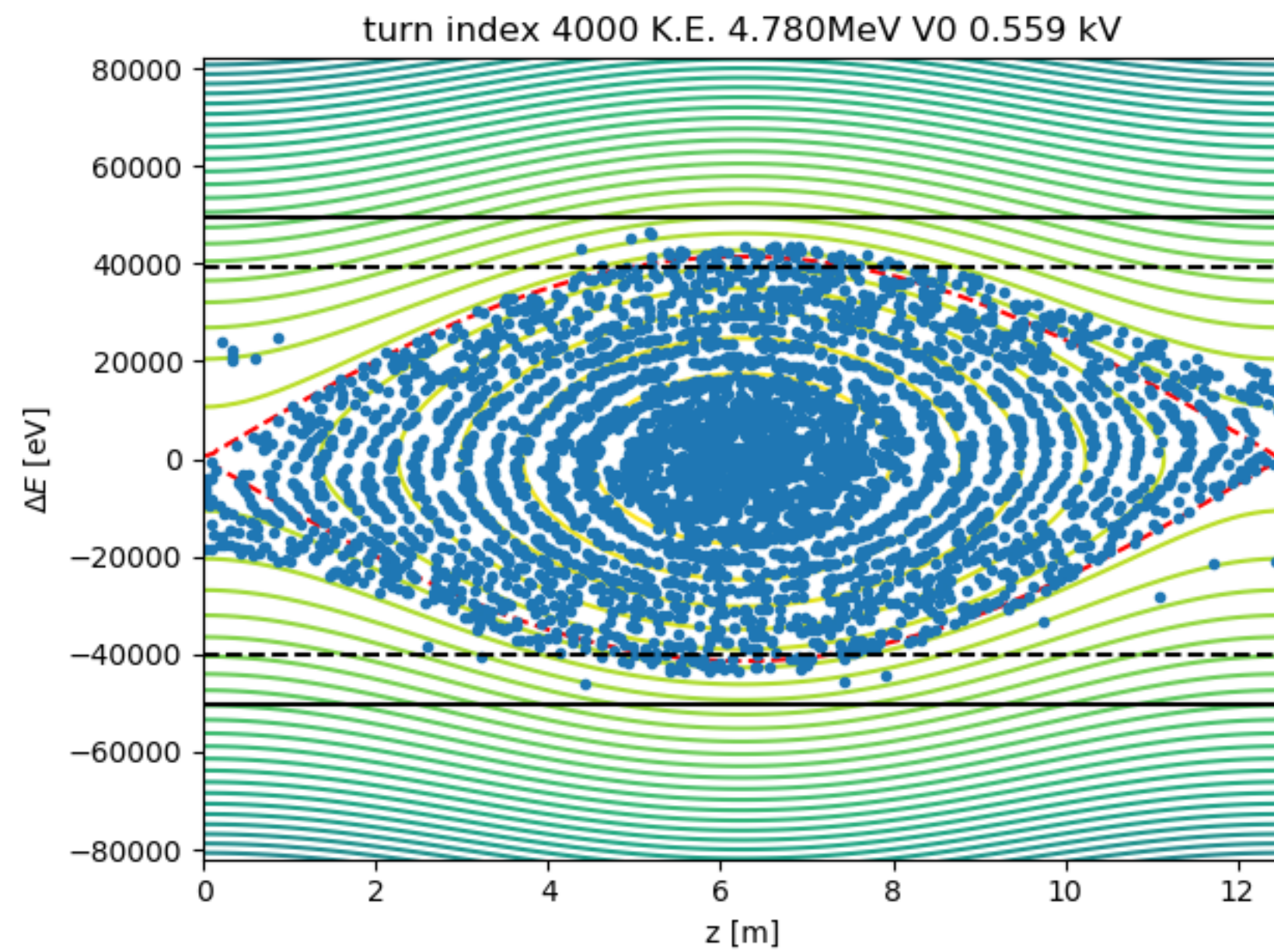
turn index 3281 K.E. 4.780MeV V0 1.988 kV



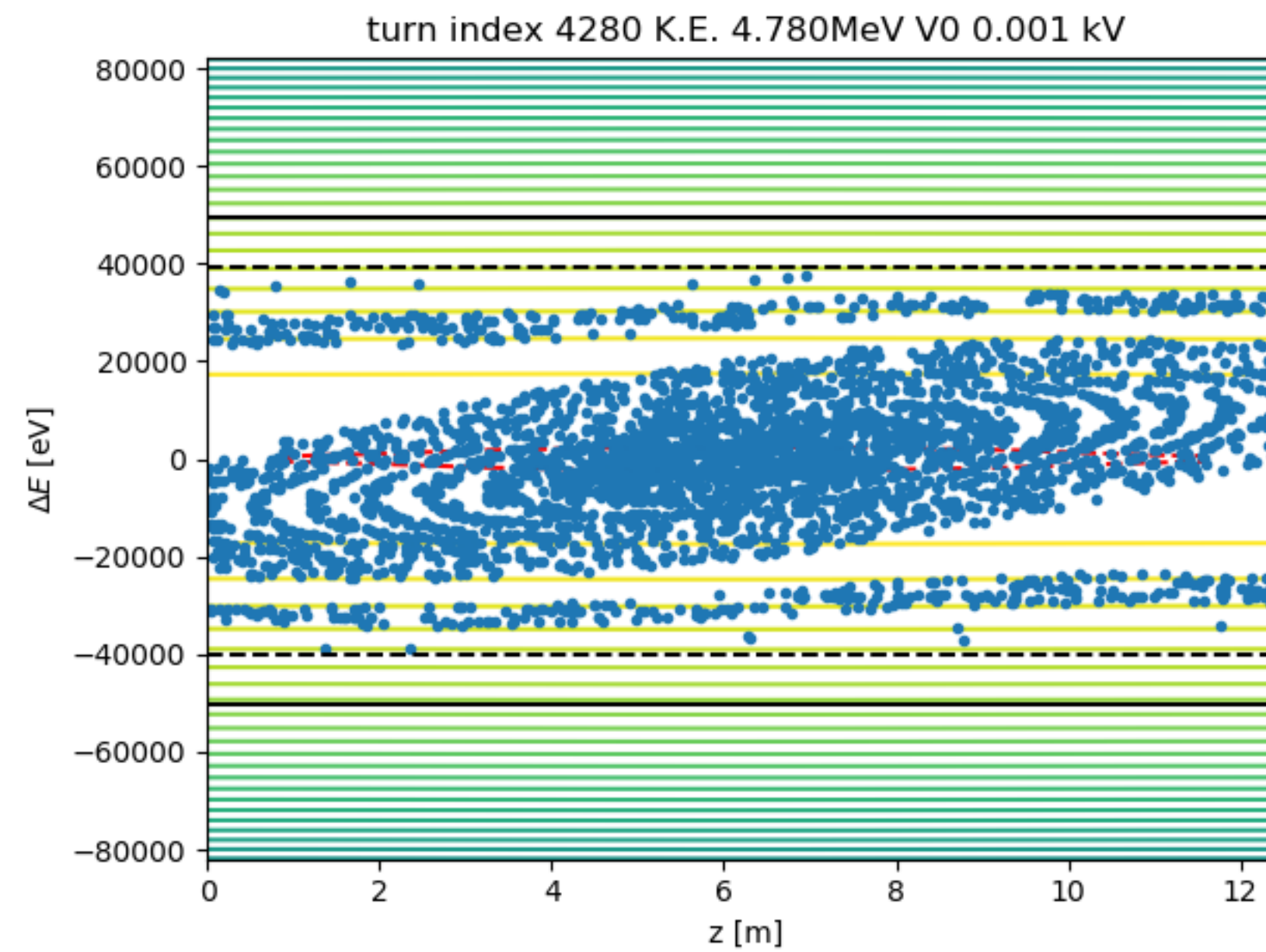
ϕ_s ramped down to zero

- Bucket area and longitudinal emittance (75% of BA) remain constant.

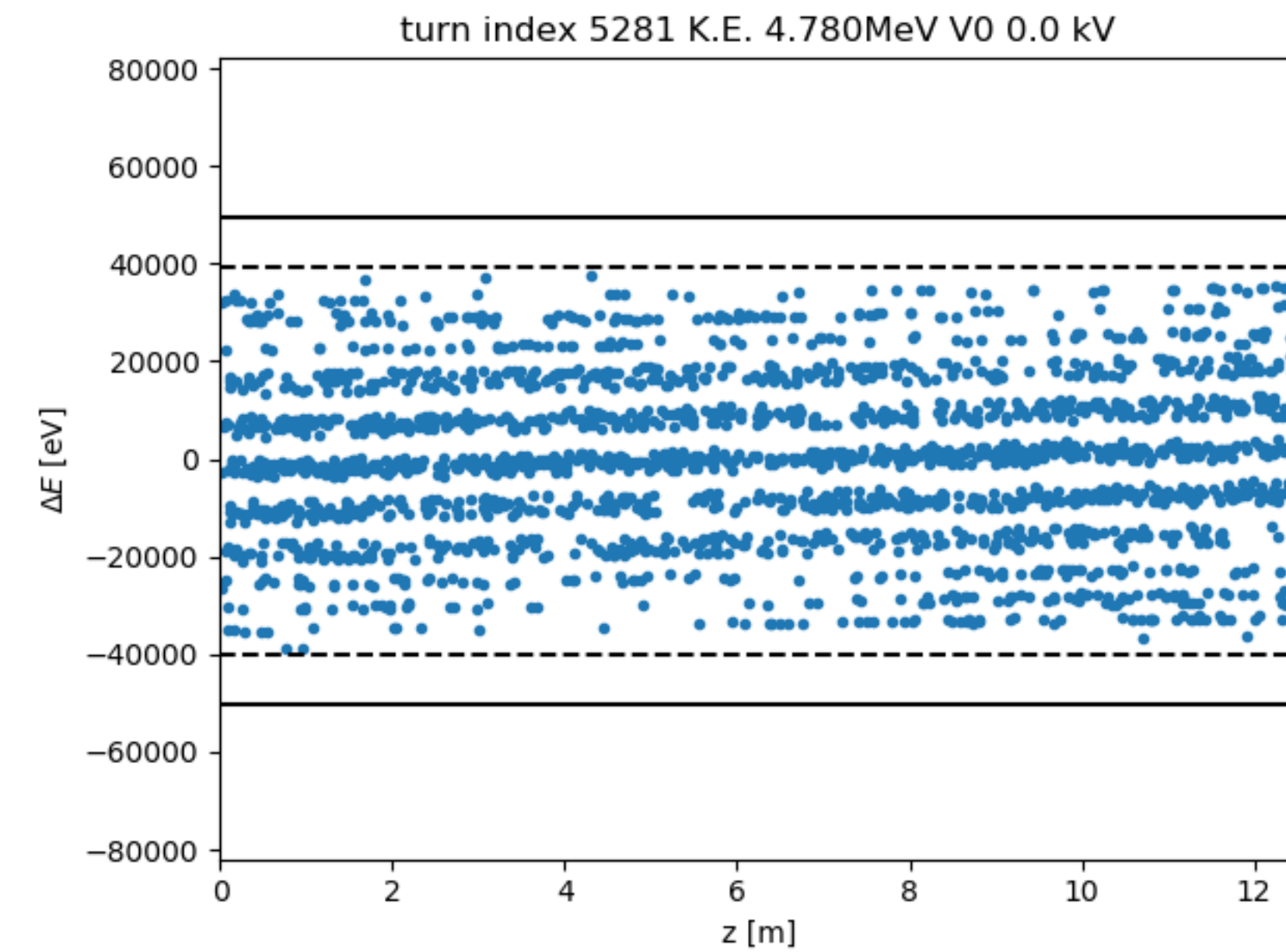
FETS-FFA: Adiabatic Debunching



RF Voltage reduced to 0.6kV



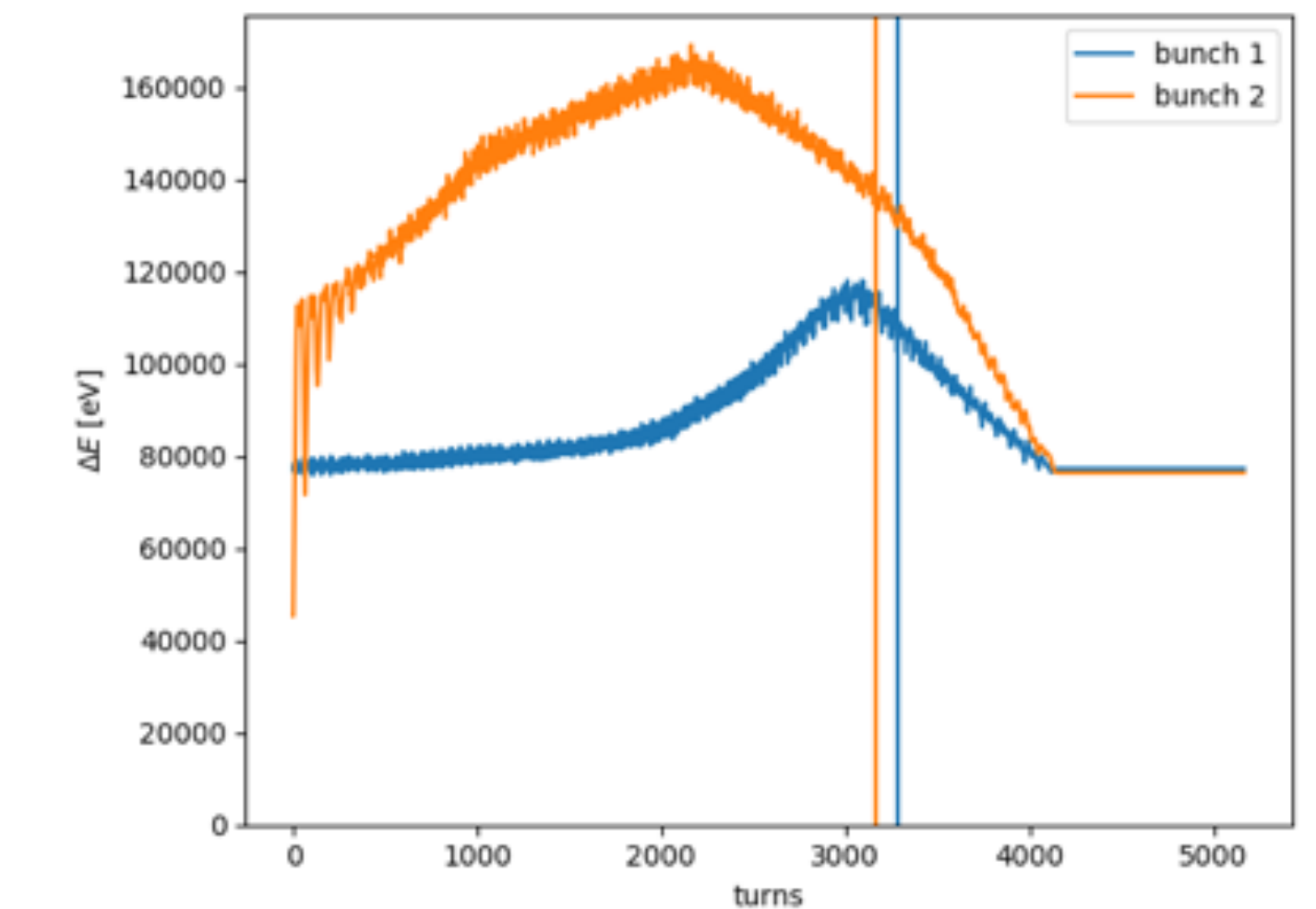
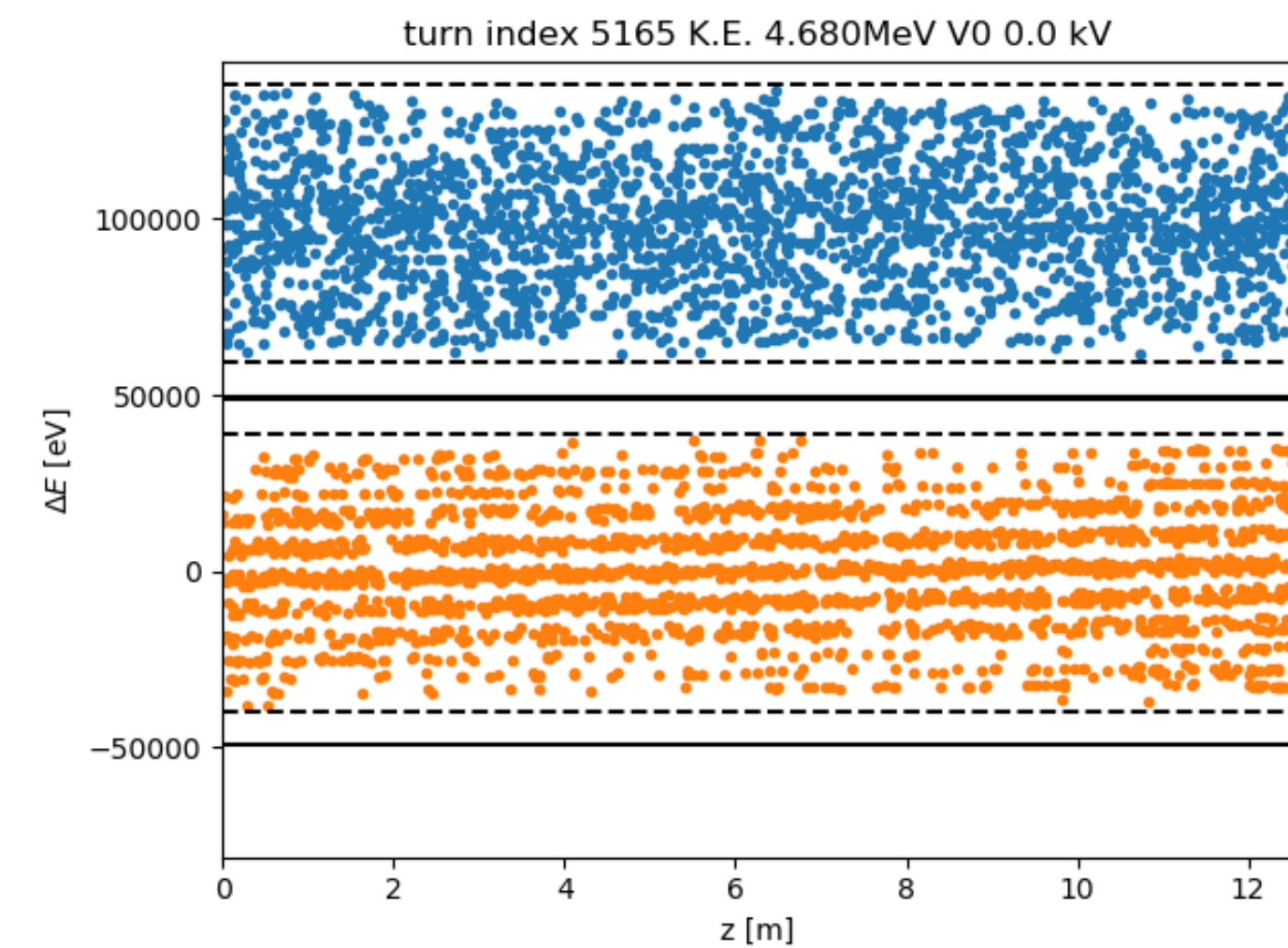
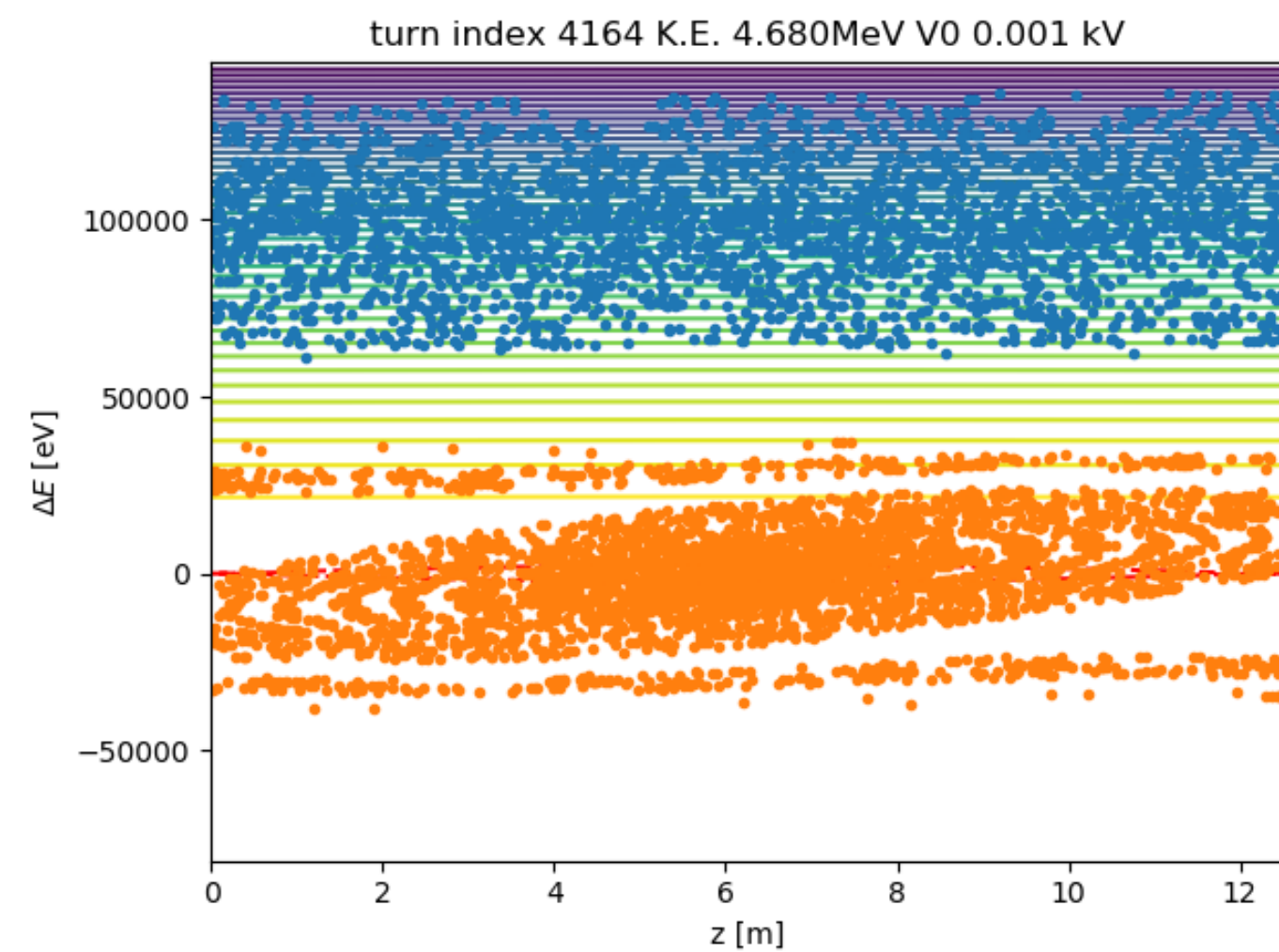
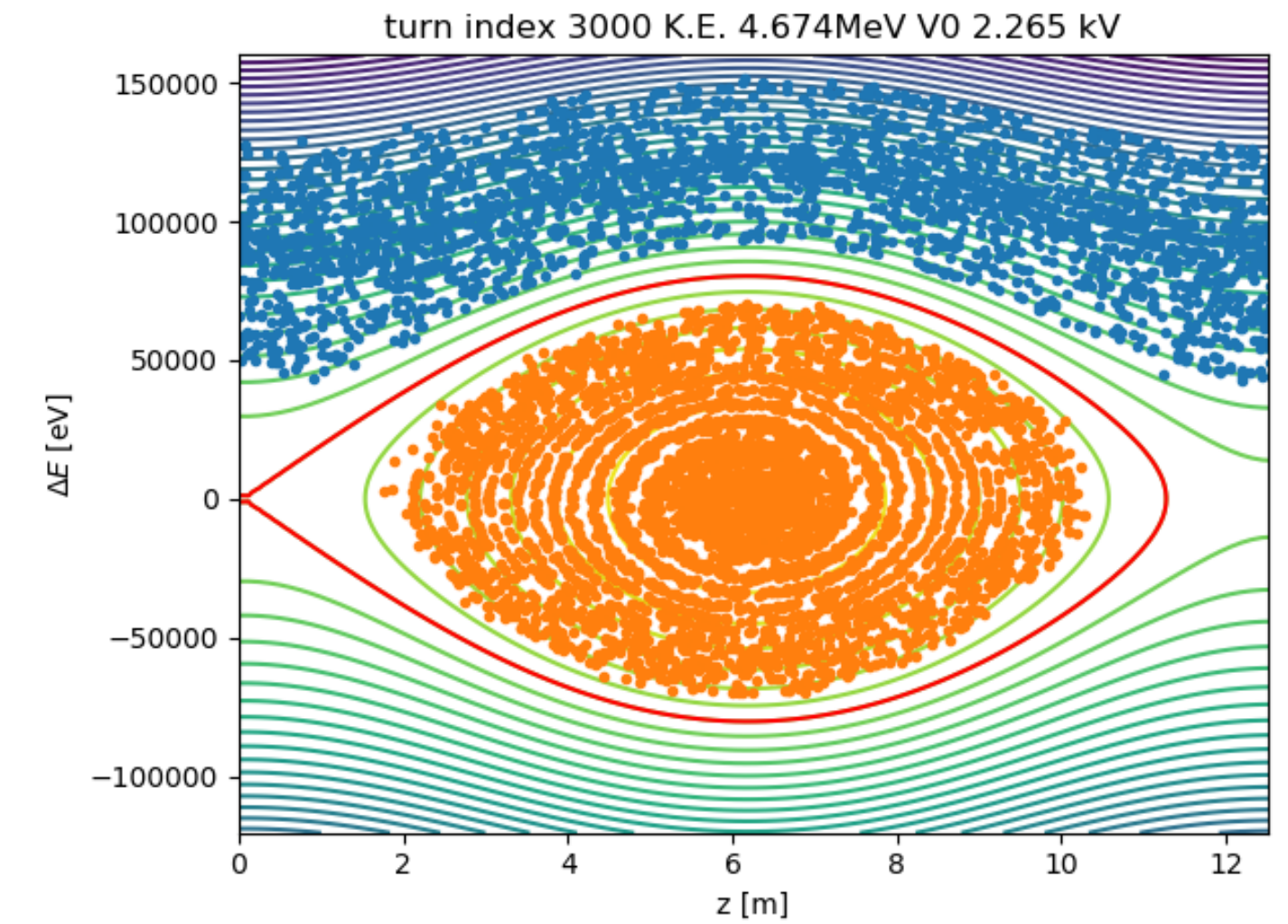
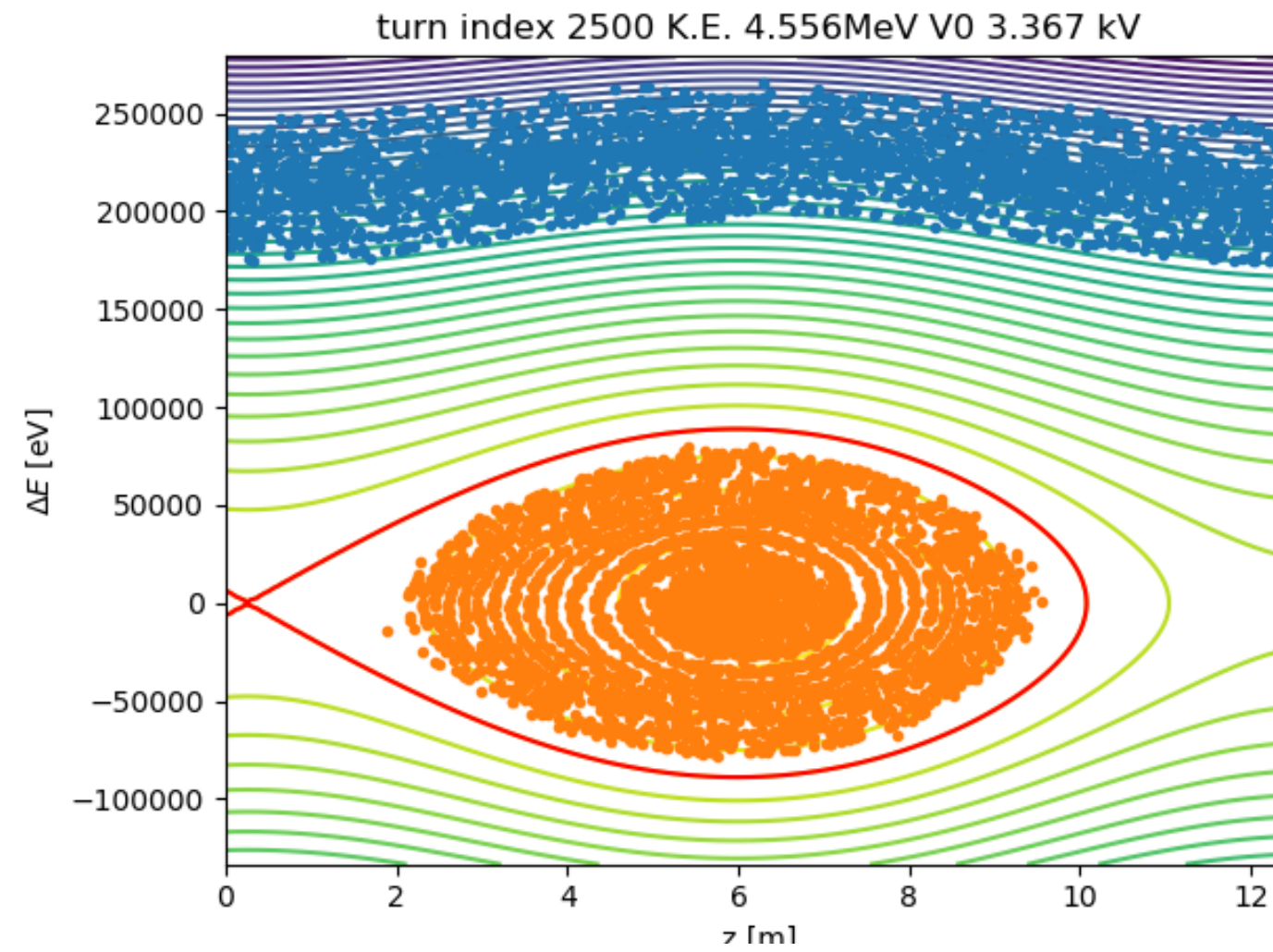
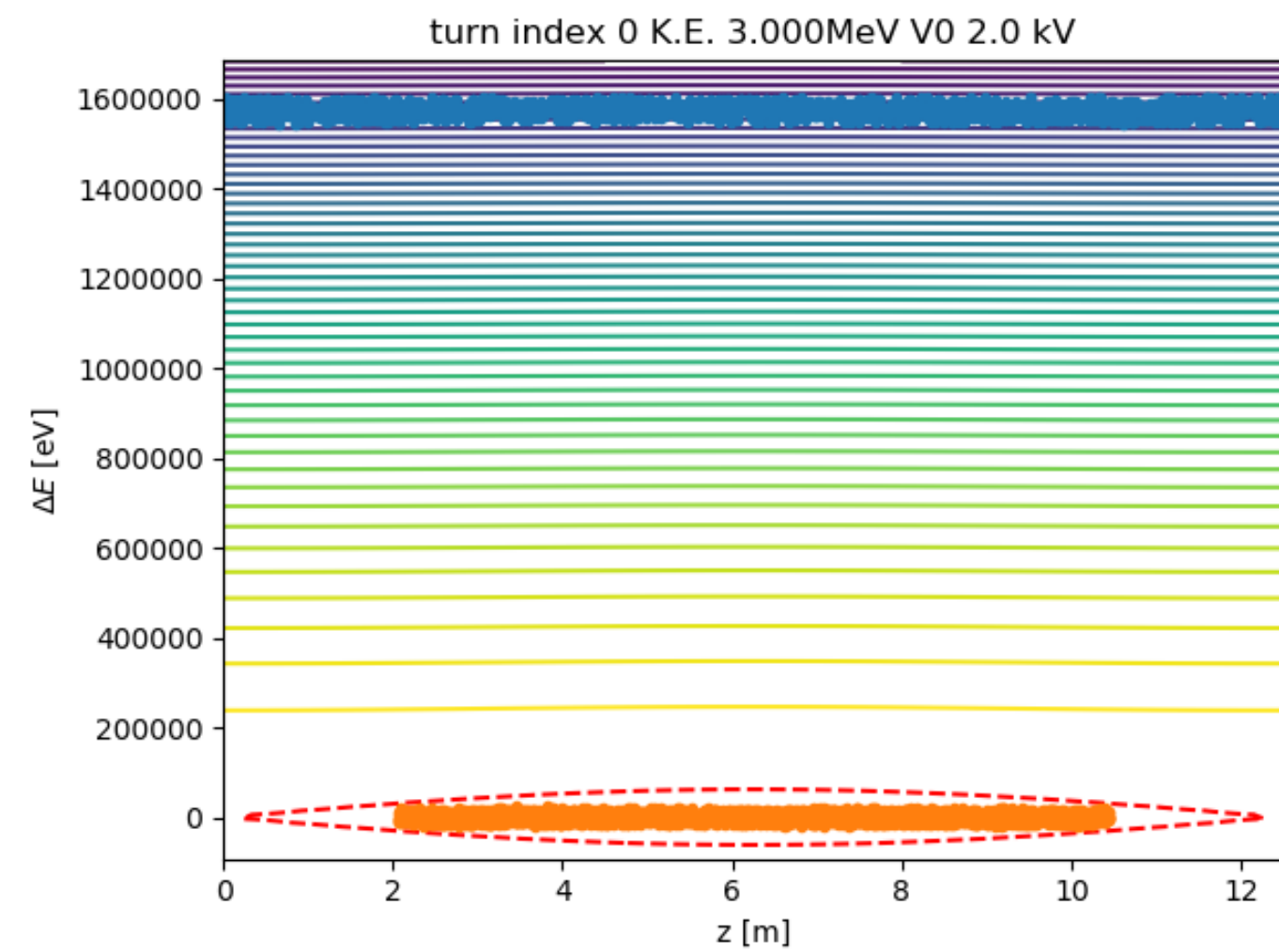
RF voltage reduced to zero



1000 turns later

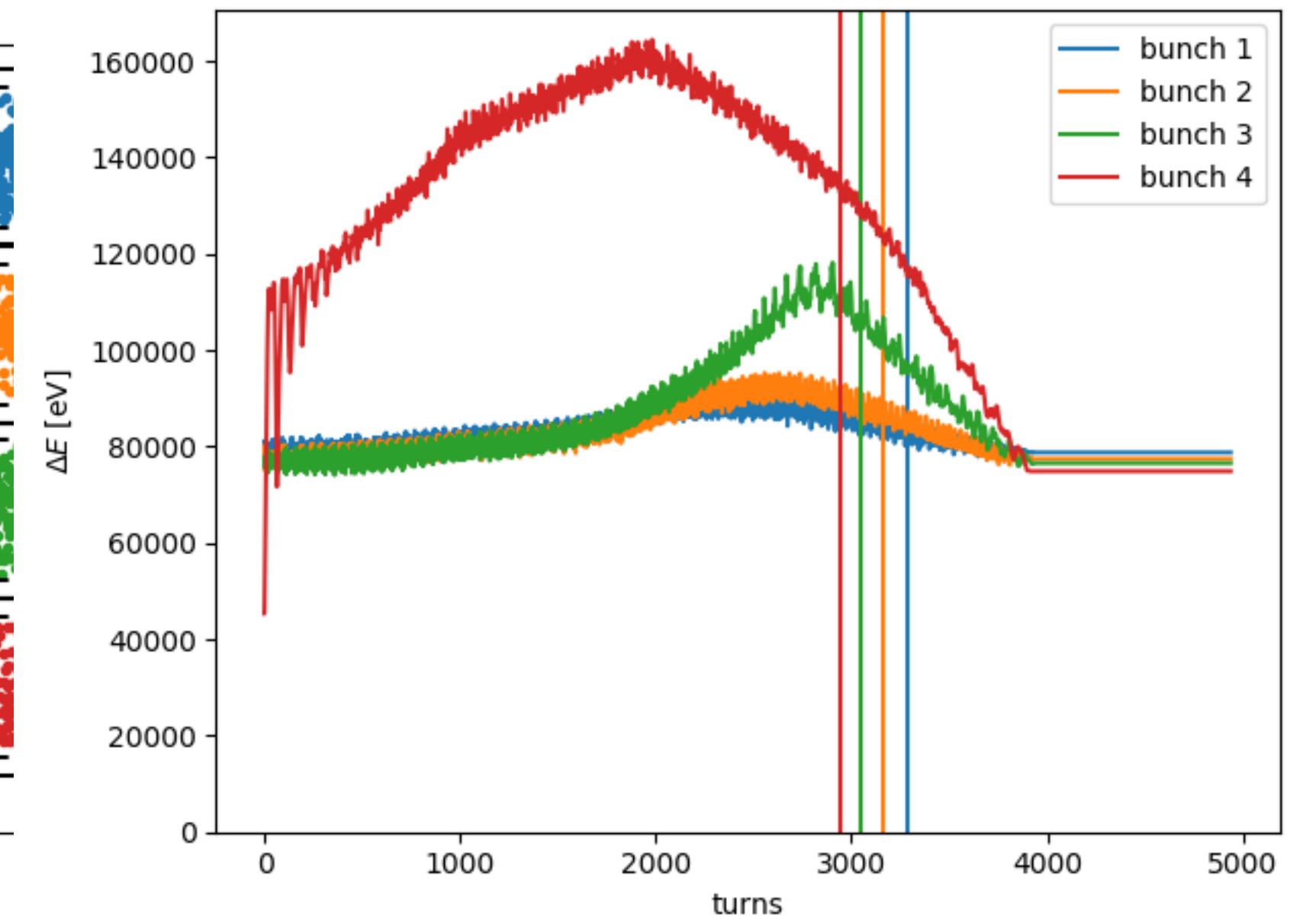
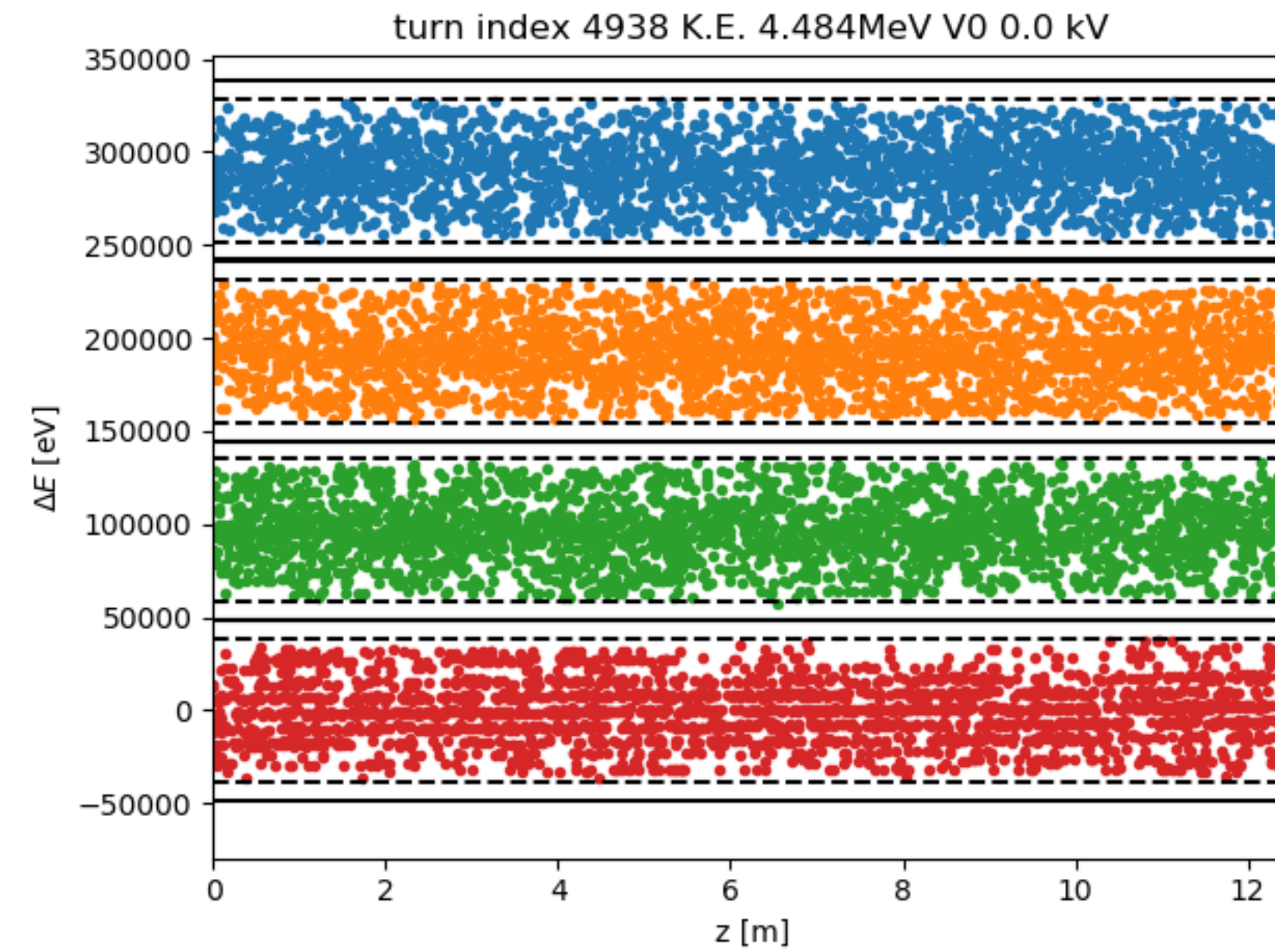
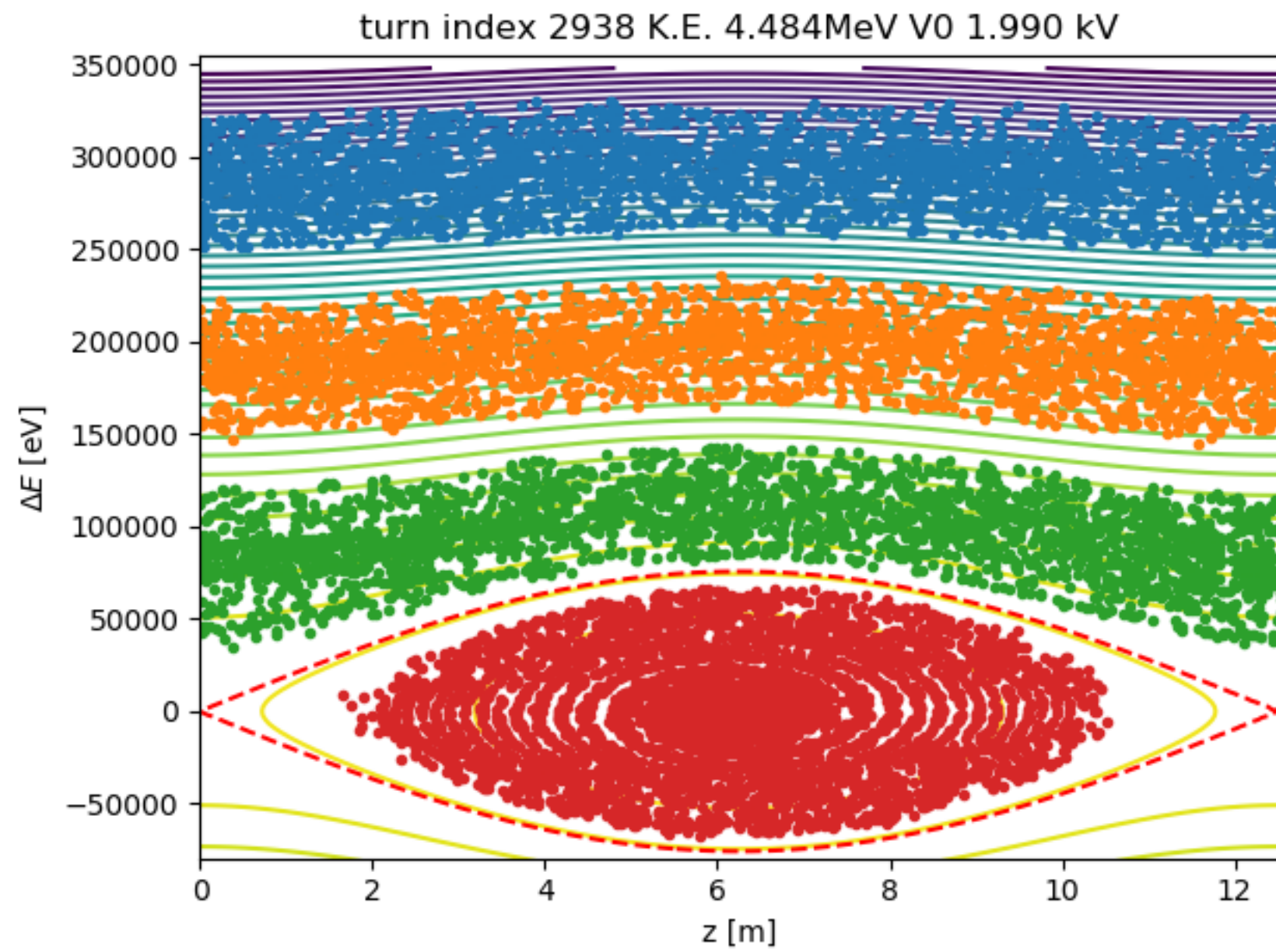
- RF voltage linearly ramped to zero in 1000 turns. The emittance is preserved.

FETS-FFA: Stack Two Beams



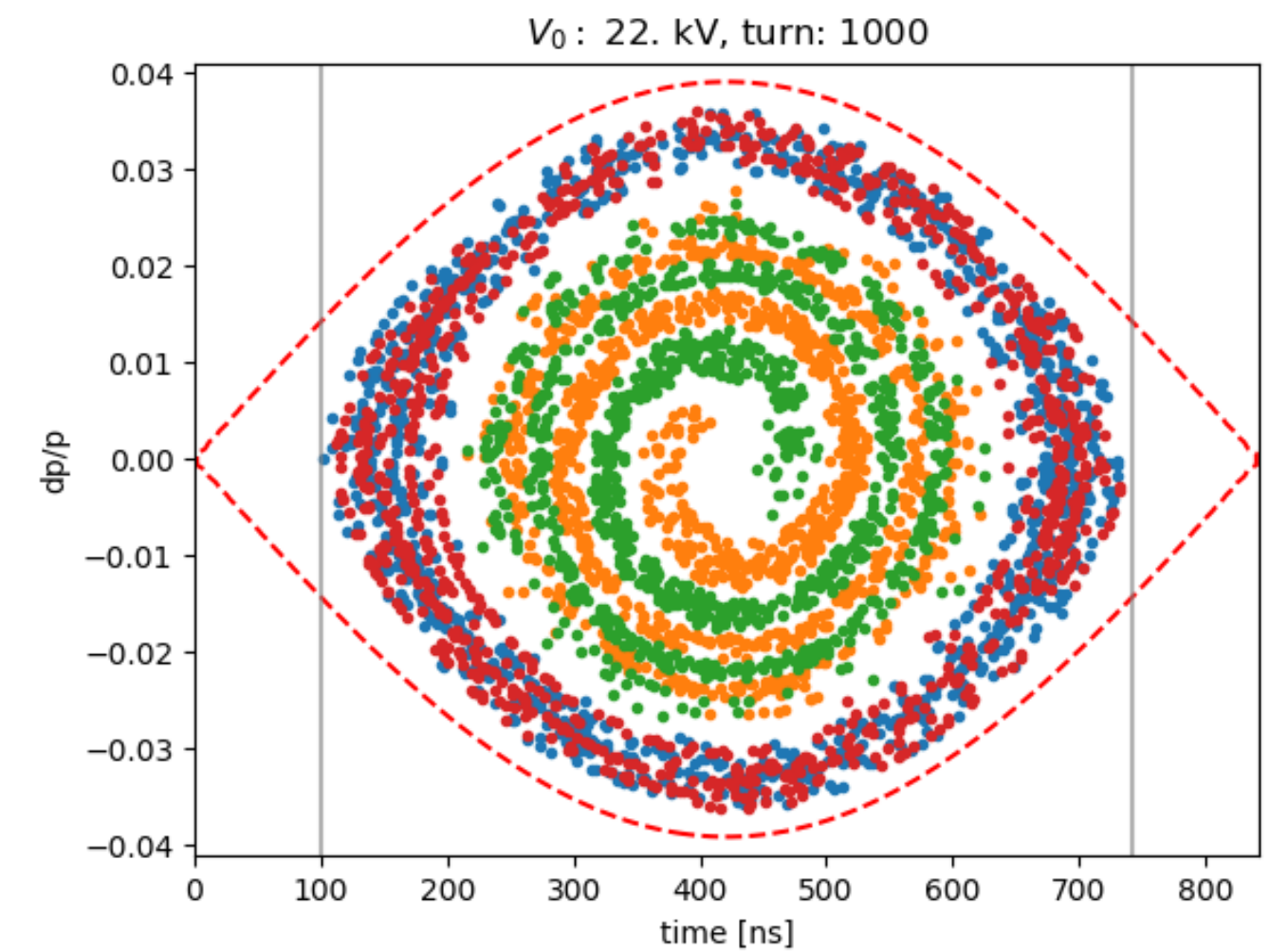
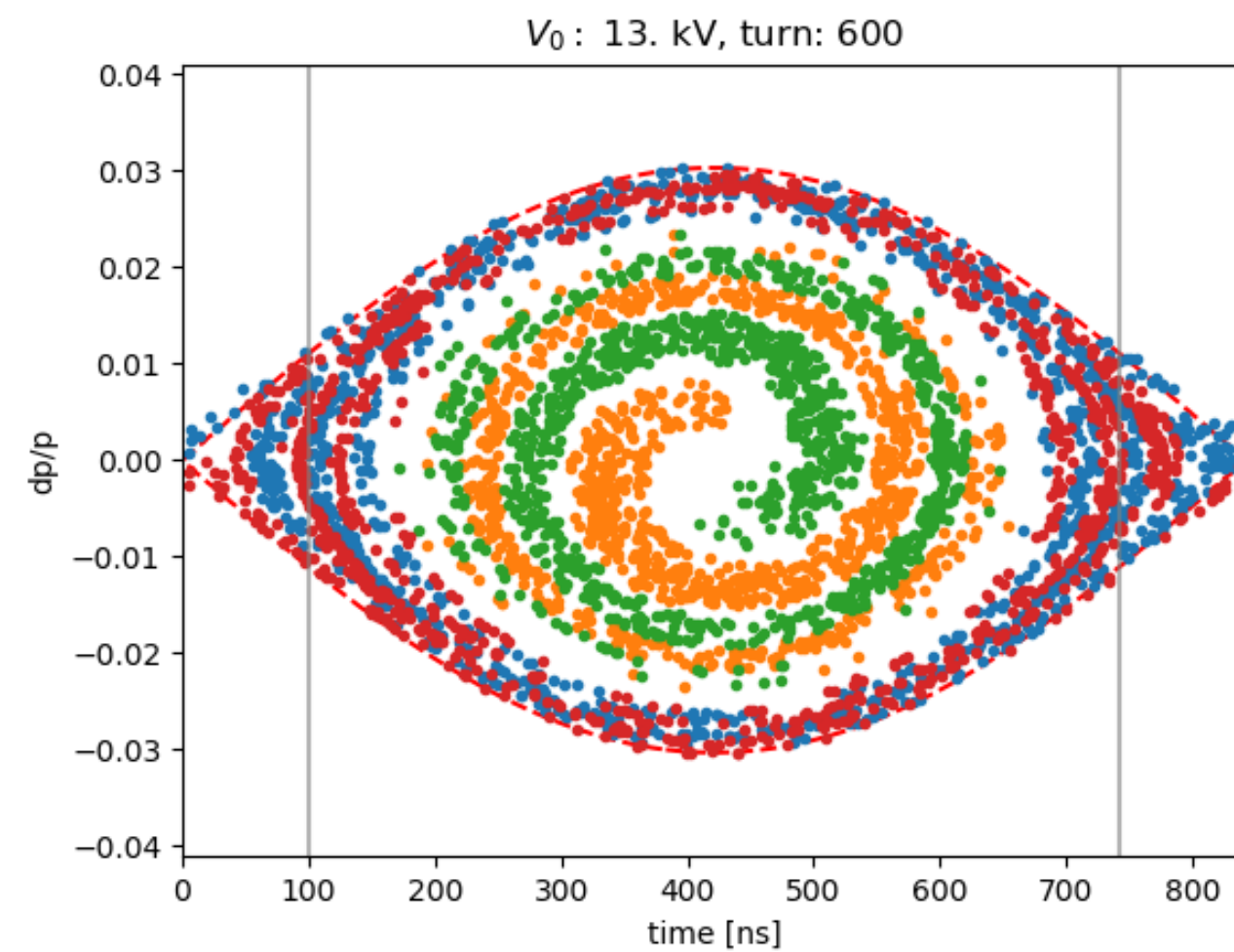
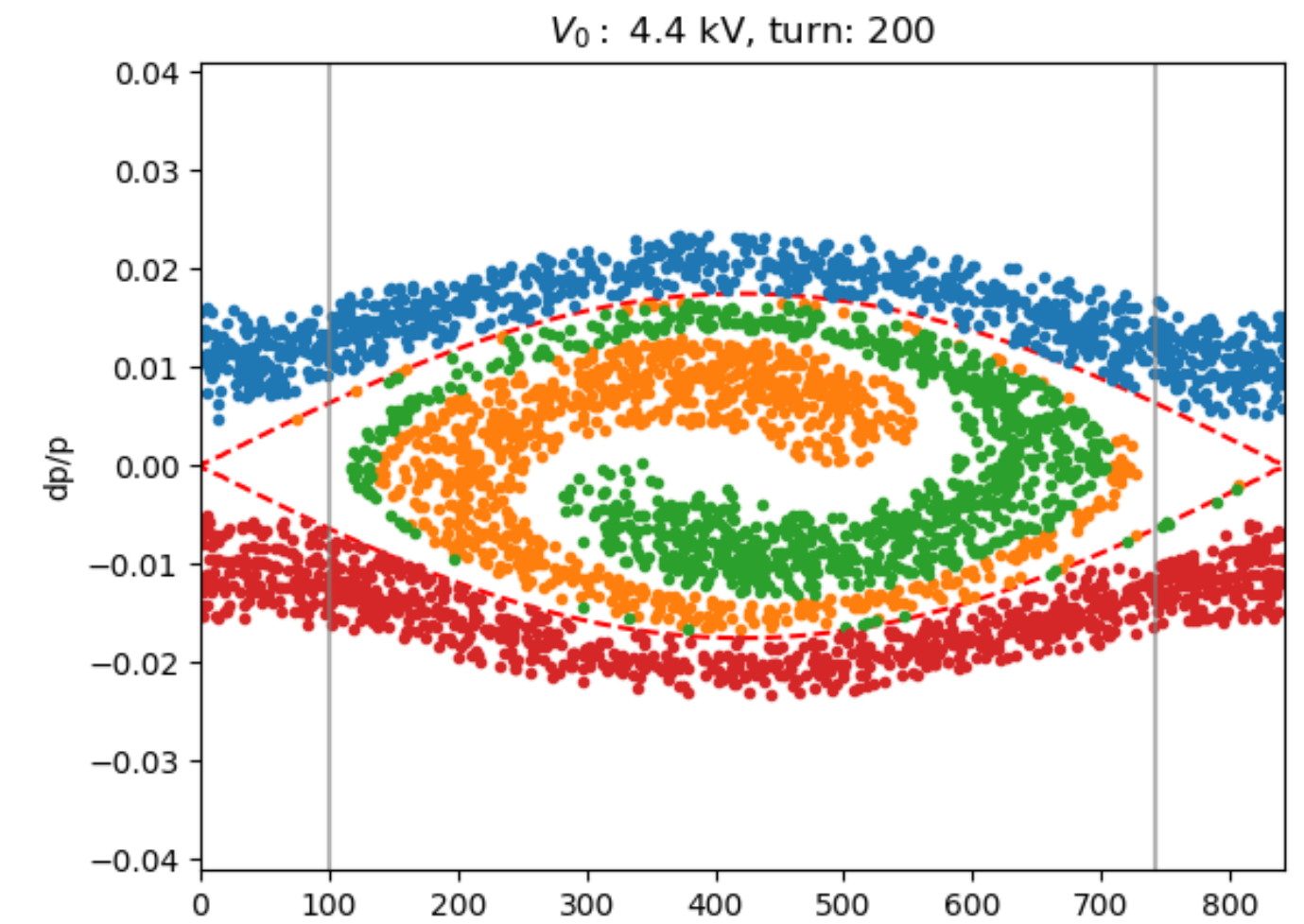
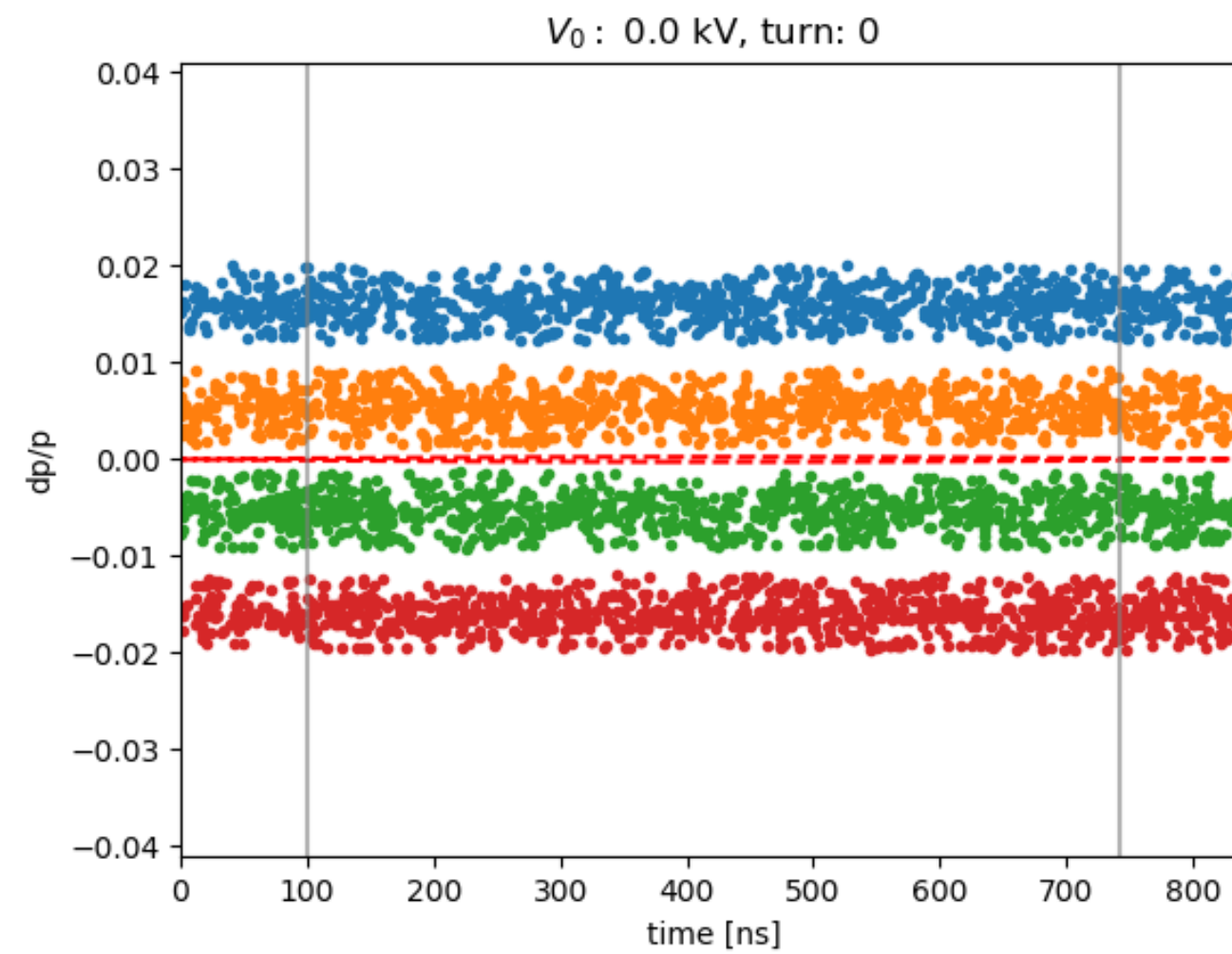
Energy spread during second bunch acceleration

FETS-FFA: Stack Four Beams



FETS-FFA: Capture

- The stacked beam must be captured before extraction.
- 22kV is enough to ensure 200ns beam-free time for the extraction kicker rise time.
- 1000 turns is sufficient to ensure the capture is adiabatic.



FETS-FFA RF Specs

3-12 MeV proton VFFA

- Plan to install one variable frequency cavity for acceleration and a separate fixed-frequency cavity for stacking.

Parameter	Value
Acceleration	
RF frequency range (h=2)	1.91 – 3.8 (4.5) MHz
RF peak voltage	4.4 (5.2) kV RF cavity design: 6kV
Stacking	
RF frequency range (h=1)	~ 1 MHz (fixed but adjustable)
RF peak voltage	35 kV (stack 5 beams)